

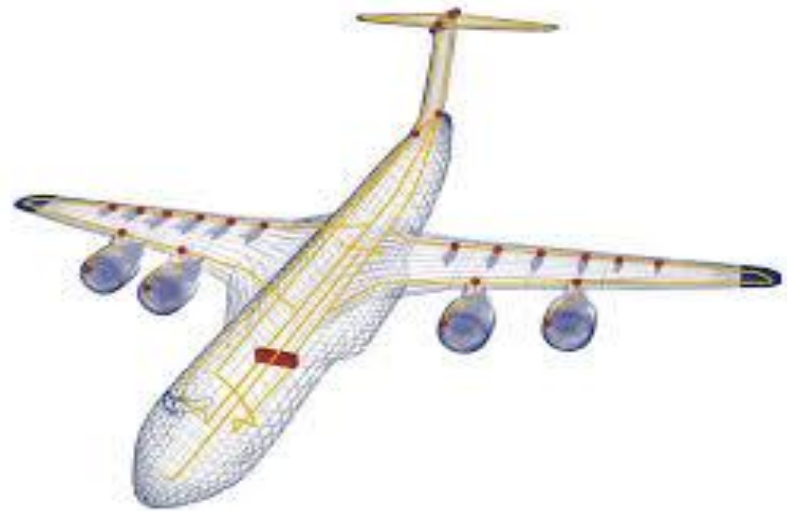
# Structural Health Monitoring in the Digital Era

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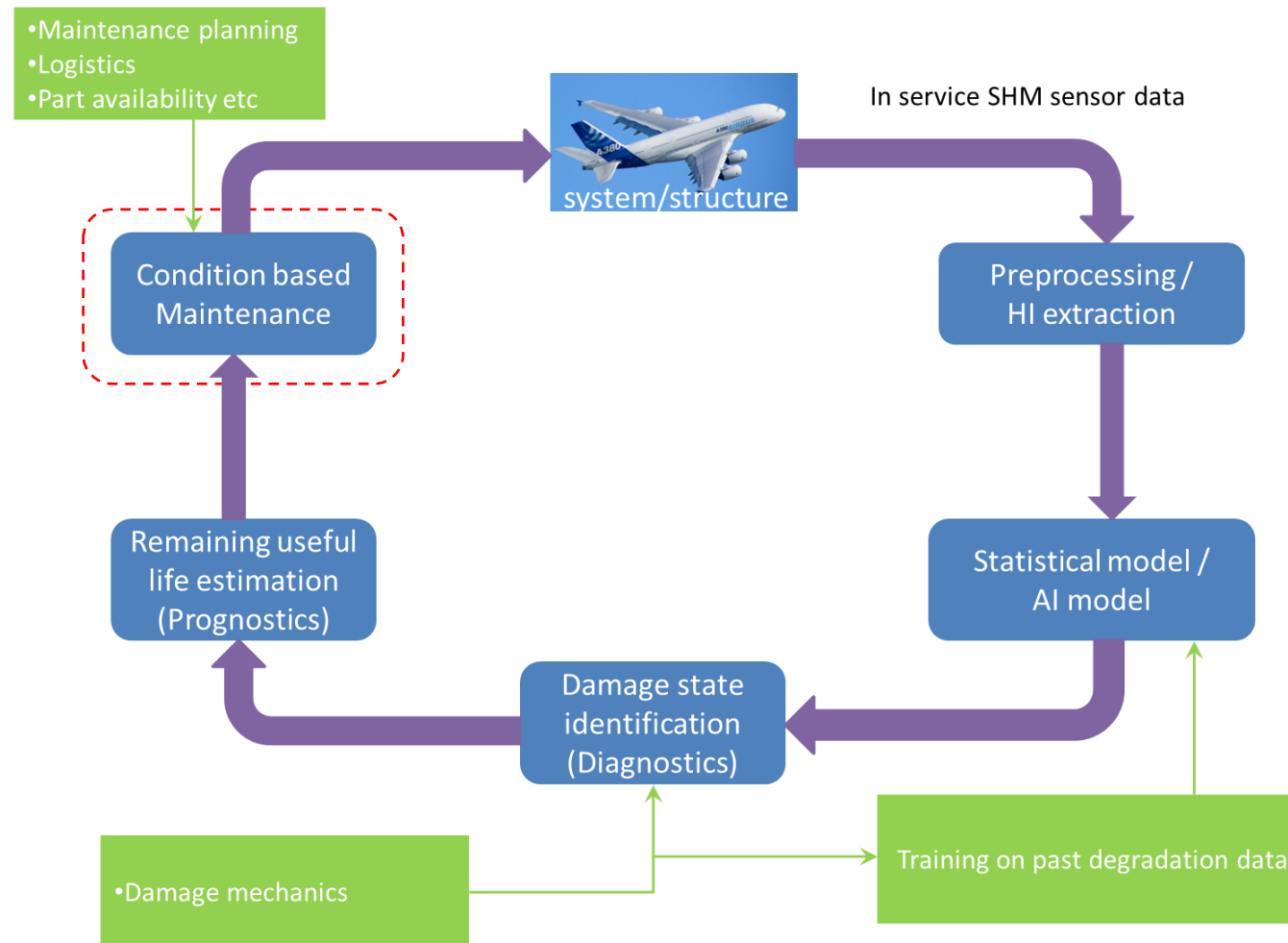
# Outline



- Definitions
- Levels of SHM
- Axioms of SHM
- SHM system design guidelines
- Sensing technologies for SHM
- Case Study I: Digital twin based SHM
- Case Study II- Remaining Useful Life Prognostics

# The vision – towards Condition Based Maintenance

The prognostication of the remaining useful life in composite structures based on SHM data

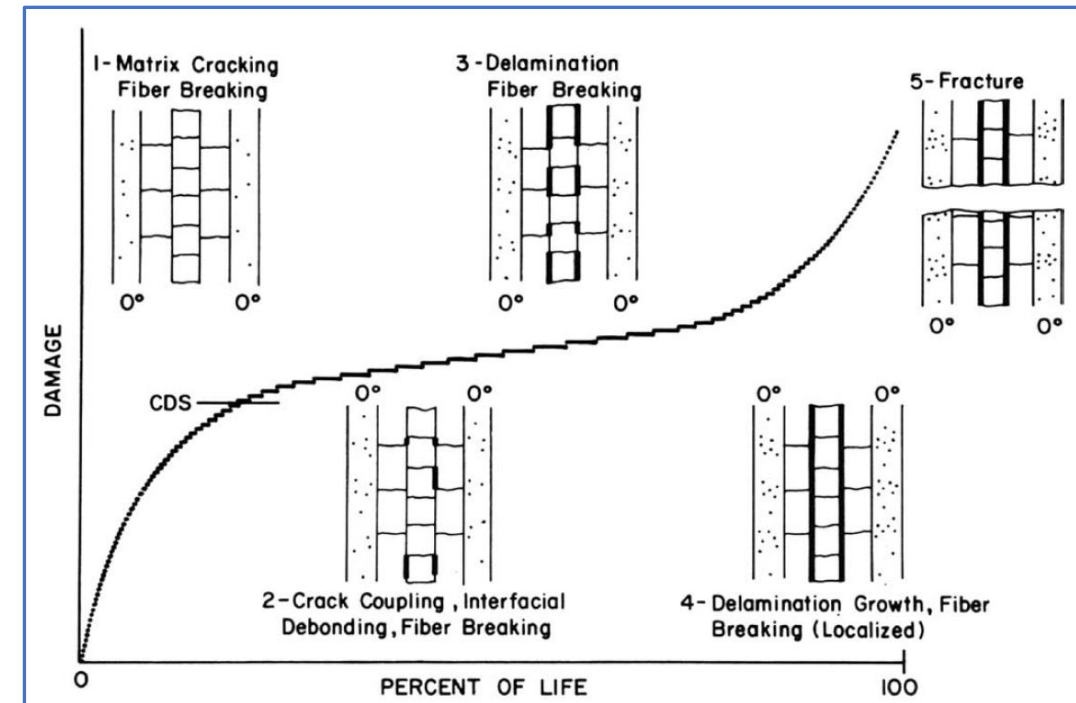


# Definitions

**Damage:** changes to the material and/or geometric properties of structures or systems, including changes to the boundary conditions, which adversely affect the current or future performance of the material

**Structural Health Monitoring:** the process of implementing a damage identification strategy for aerospace, civil and mechanical engineering infrastructure

*Damage accumulation  
in a composite's lifetime  
(Reifsnider early 1980s)*



# Levels of SHM

## Non-destructive testing

### Level 5

Self-healing

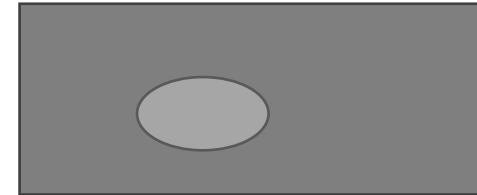
- Introduce damage restoration mechanisms



### Level 4

Remaining Lifetime

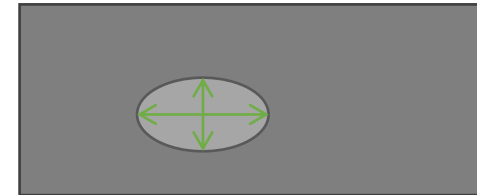
- Prognosis of the remaining service life of the structure



### Level 3

Sizing of Damage

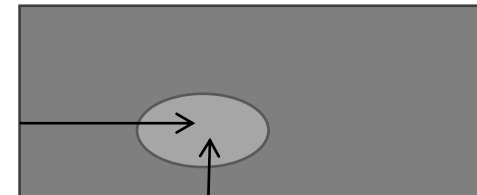
- Quantification of the severity of the damage



### Level 2

Locating Damage

- Determination of the geometric location of the damage



### Level 1

Anomaly detection

- Determination that damage is present in the structure



# Fundamental axioms of SHM\*

**Axiom I:** All materials have inherent flaws or defects. Service loading induces new faults or propagates existing ones

**Axiom II:** The assessment of damage requires a comparison between two system states.

**Axiom III:** Identifying the existence and location of damage (i.e. Levels I & II) can be done in an unsupervised learning mode, but identifying the type of damage present and the damage severity (i.e. Levels III & IV) can generally only be done in a supervised learning mode.

**Axiom IVa:** Sensors cannot measure damage. Feature extraction through signal processing and statistical classification is necessary to convert sensor data into damage information.

**Axiom IVb:** Without intelligent feature extraction, the more sensitive a measurement is to damage, the more sensitive it is to changing operational and environmental conditions.

**Axiom V:** The length- and time- scales associated with damage initiation and evolution dictate the required properties of the SHM sensing system.

**Axiom VI:** There is a trade-off between the sensitivity to damage of an algorithm and its noise rejection capability.

**Axiom VII:** The size of damage that can be detected from changes in system dynamics is inversely proportional to the frequency range of excitation.

*\*Worden et al., Proceedings of The Royal Society A, 2007*

# SHM system design guidelines

- (i) Sensor types, number and locations
- (ii) Bandwidth, sensitivity and dynamic range
- (iii) Data acquisition/telemetry/storage system
- (iv) Power requirements
- (v) Sampling intervals (continuous monitoring versus monitoring only after extreme events or at periodic intervals)
- (vi) Processor/memory requirements
- (vii) Excitation source (active sensing)

# SHM system design parameters

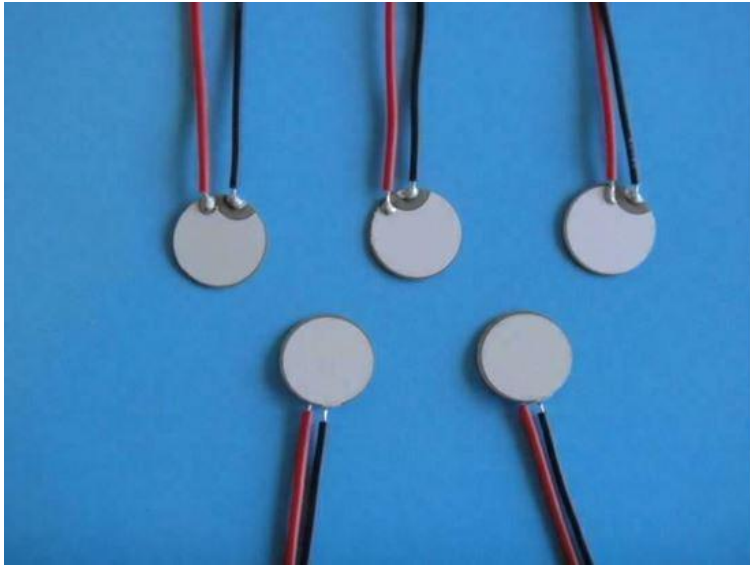
- (i) The length-scales on which damage is to be detected (global vs local approaches)
- (ii) The time-scale on which damage evolves (milliseconds vs hrs of flight)
- (iii) How will varying and/or adverse operational and environmental conditions affect the sensing system
- (iv) Cost



# Sensing technologies for SHM

1. Piezoelectric (PZT)
2. Fibre optic sensors (Fibre Bragg Gratings, distributed sensing)
3. Accelerometers
4. Acoustic Emission
5. Classical strain gauges
6. Temperature sensors
7. Hybrid schemes and others

# 1. PZTs (Piezoceramic elements)



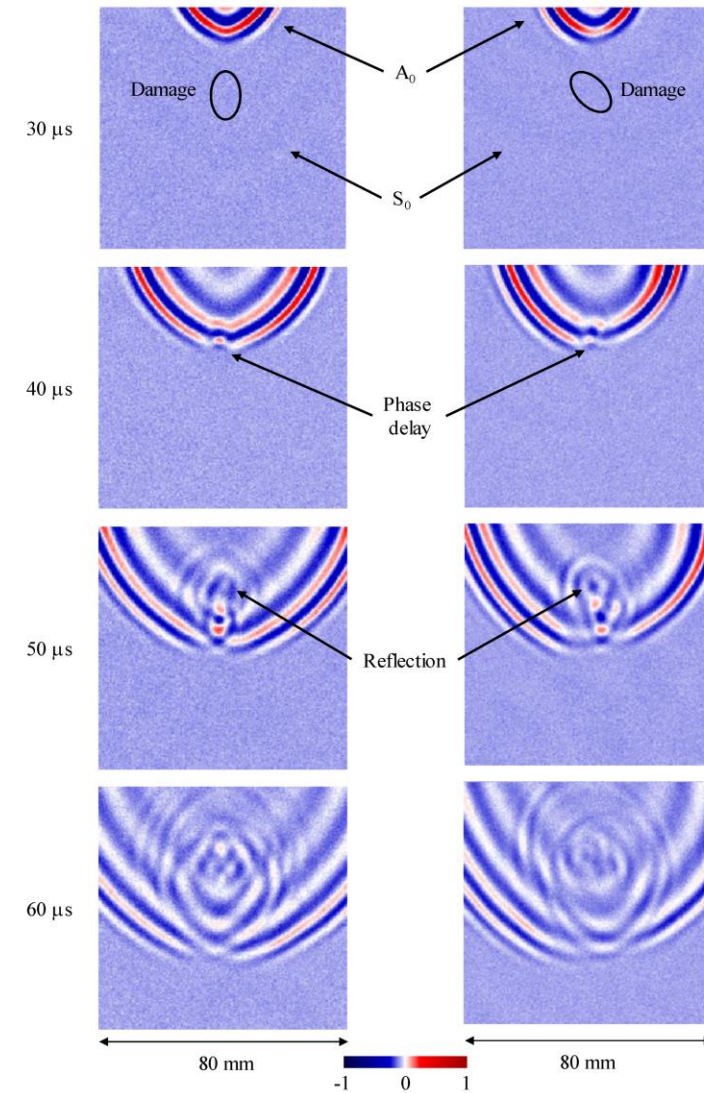
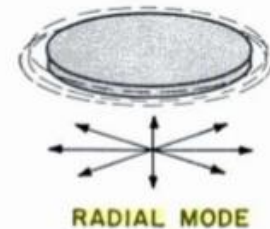
## Modes of Vibration

2 TYPES:

### 1. thickness mode

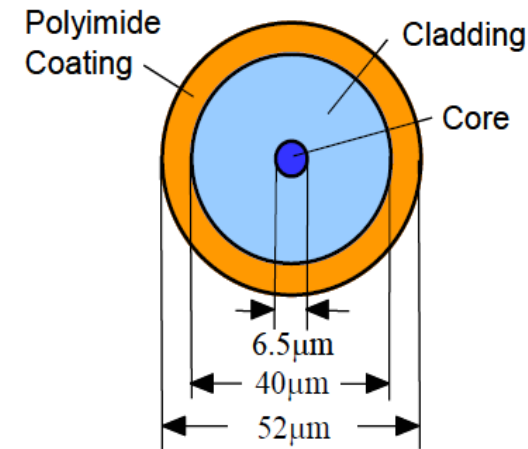
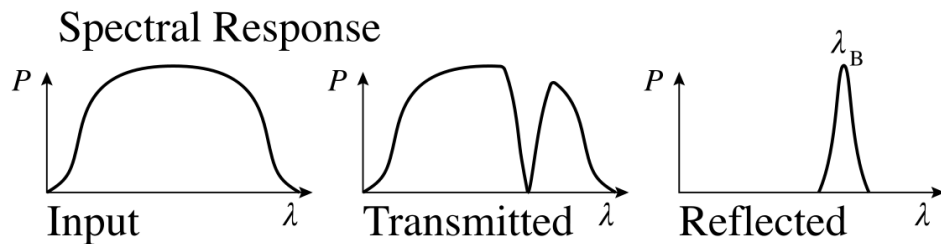
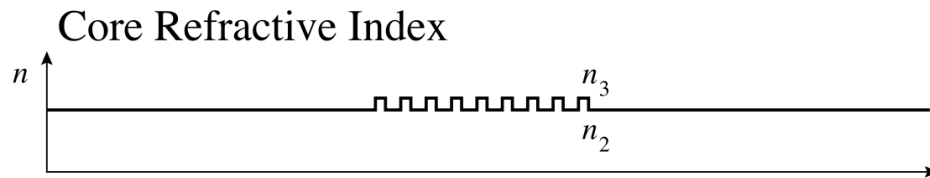
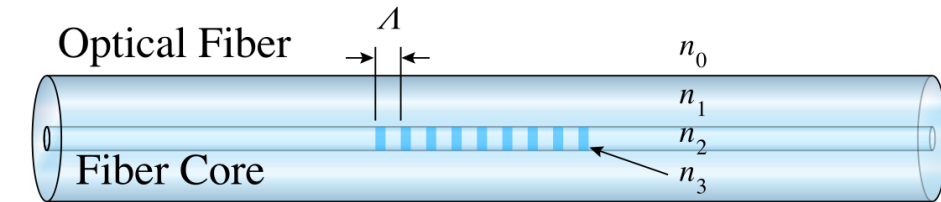
- most common
- Used in medical crystals

### 2. radial mode



*Toyama et al. Appl. Sci. 2019*

## 2. Optical fiber sensors (Fiber Bragg sensors)



Fiber grating is made by periodically changing the refractive index in the glass core of the fiber. The refractive changes are made by exposing the fiber to UV-light with a fixed pattern.

$$\Delta\lambda_B = 2n\Lambda \left[ \left\{ 1 - \left( \frac{n^2}{2} \right) \left[ P_{12} - \nu (P_{11} + P_{12}) \right] \right\} \varepsilon + \left[ \alpha + \frac{\left( \frac{dn}{dT} \right)}{n} \right] \Delta T \right]$$

## 2. Optical fiber sensors (Distributed sensing)



Distributed sensing is a technology (based on Brillouin scattering) that enables very dense, real-time measurements along the entire length of a fibre optic cable. Unlike traditional sensors that rely on discrete sensors measuring at pre-determined points, distributed sensing does not rely upon manufactured sensors but utilizes the optical fibre. The optical fibre is the sensing element without any additional transducers in the optical path.

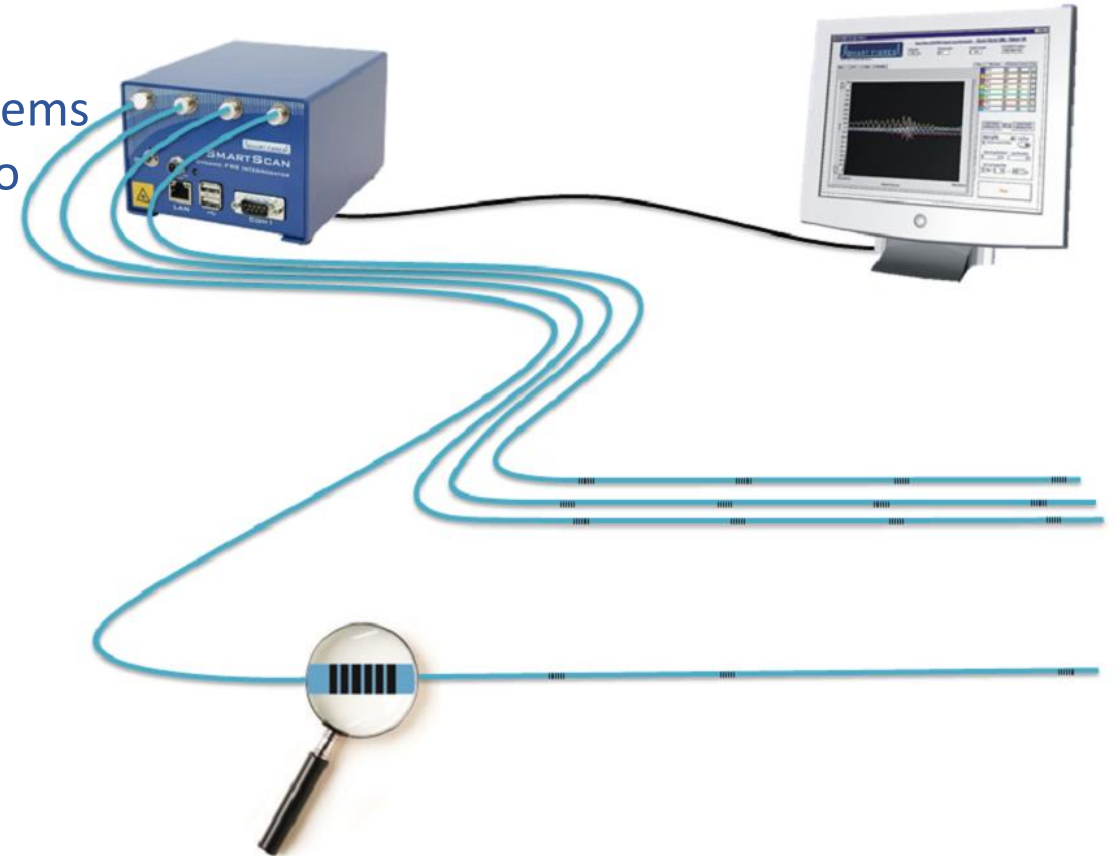
As the fibre is the sensor, it is also a cost-effective method that can be easily deployed even in the harshest and most unusual environments.

## 2. Optical fiber sensors

### Advantages:

- Small size and easy integration into a wide variety of systems
- Electrically immune, no conduction of electric current, no spark peril
- Capacity for static and/or dynamic measurements
- Immune to electromagnetic interference and radio frequency interference
- Light in weight
- Ideal for harsh environments
- High sensitivity
- Multiplexing capability thus forms sensing networks
- Remote sensing capability

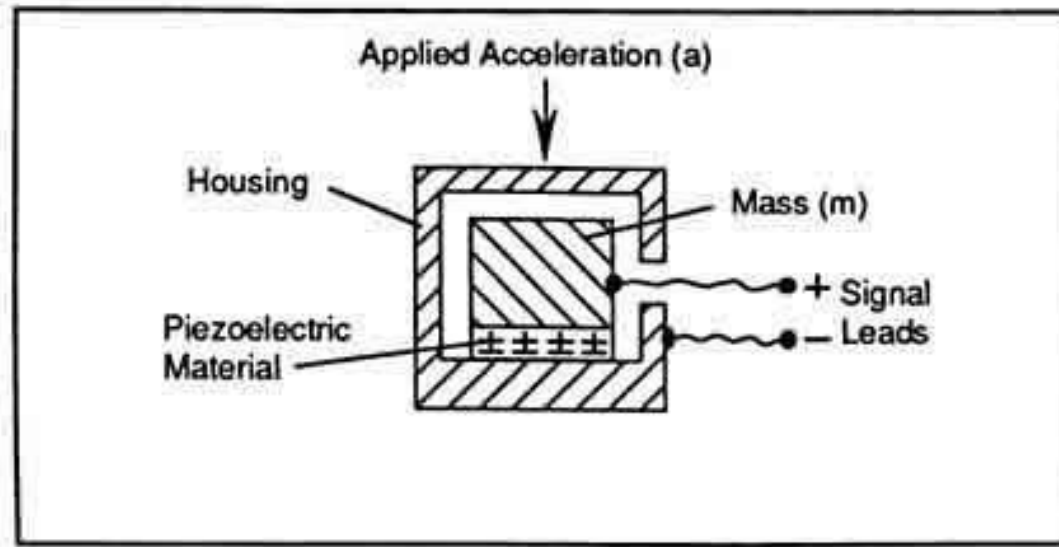
Interrogation unit (laser source) required





# 3. Accelerometers

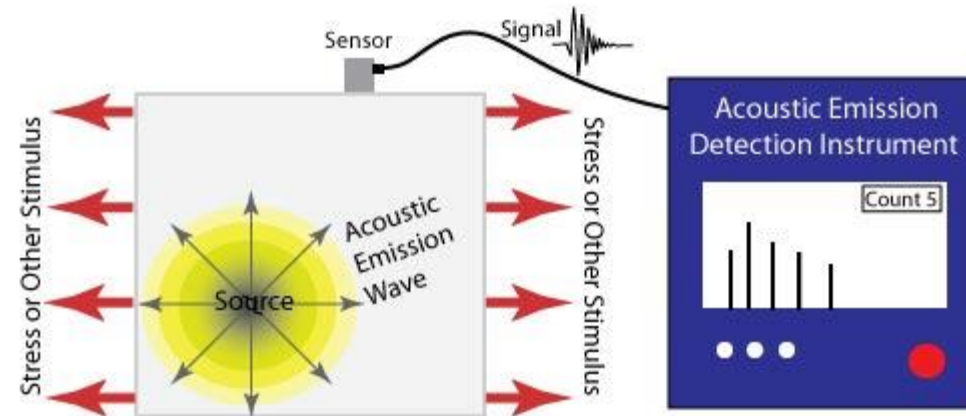
## Working principle



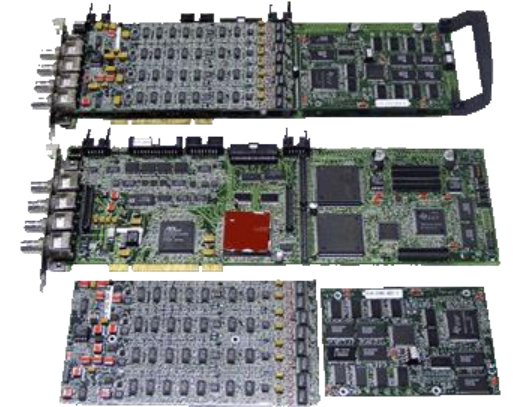
Very popular for structural dynamic measurements (vibrations)

# 4. Acoustic emission

Acoustic Emission (AE) refers to the generation of transient elastic waves produced by a sudden redistribution of stress in a material, usually in locations of defects or discontinuities.



A/D boards

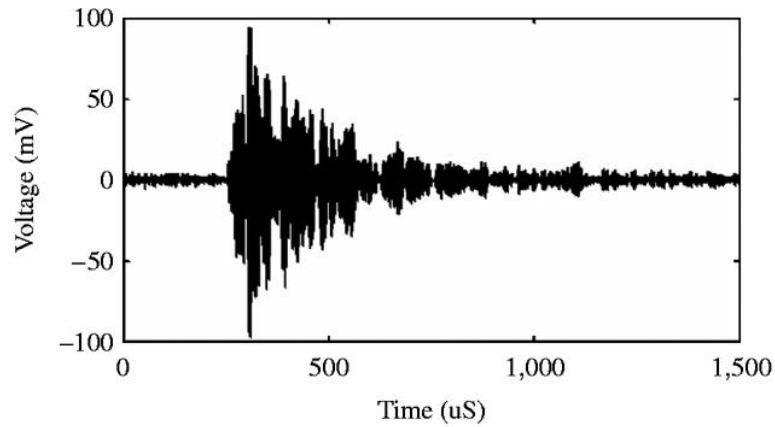


AE sensors

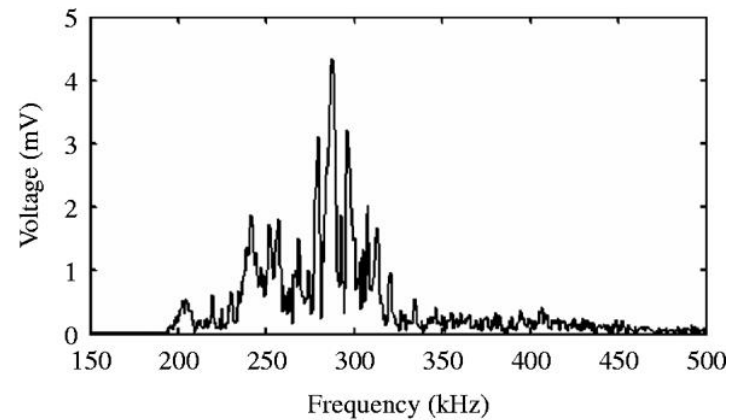


# 4. Acoustic emission

Typical waveform (burst type)



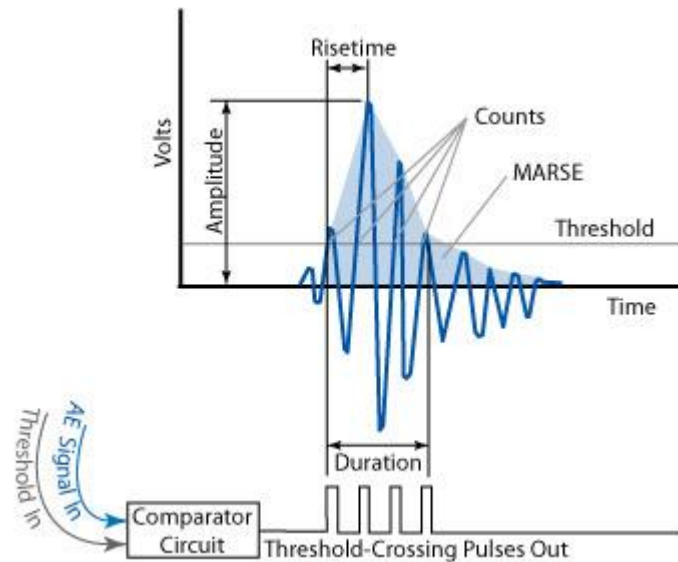
Power spectrum



Typical features

AE feature	Symbol	Unit
Duration	DUR	us
Counts	CNT	#
Amplitude	AMP	dB
Counts to peak	CNP	#
Risetime	RT	us
Energy	E	pJ
Absolute energy	ABE	fJ
Signal strength	SS	pVs
Rise angle	RAN	deg
Decay angle	DAN	deg
Average frequency	AF	kHz
Initiation frequency	INF	kHz
Reverberation frequency	REVF	kHz
FFT amplitude	FFTAMP	-
FFT peak frequency	FFTPF	kHz

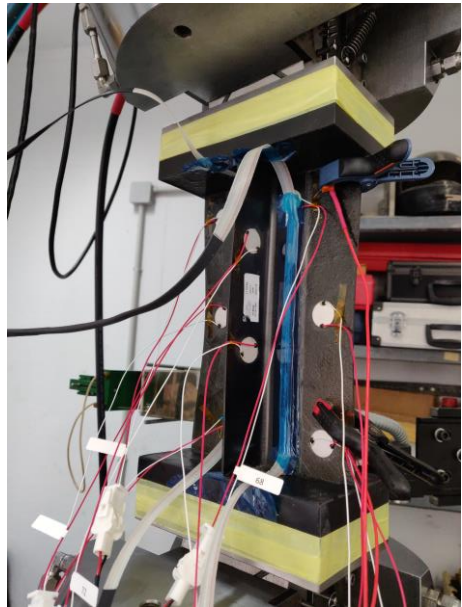
Feature extraction



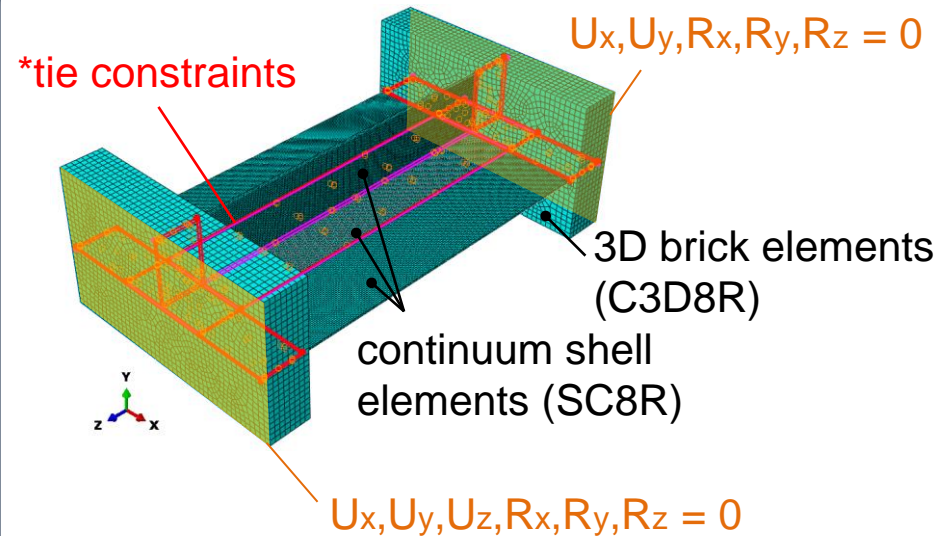
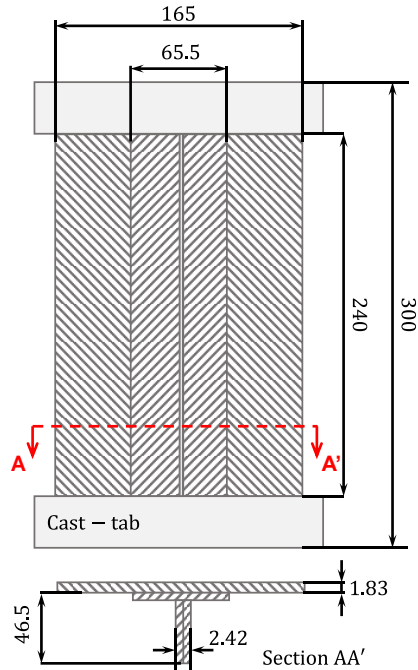


# CASE STUDY I: Digital twin based SHM

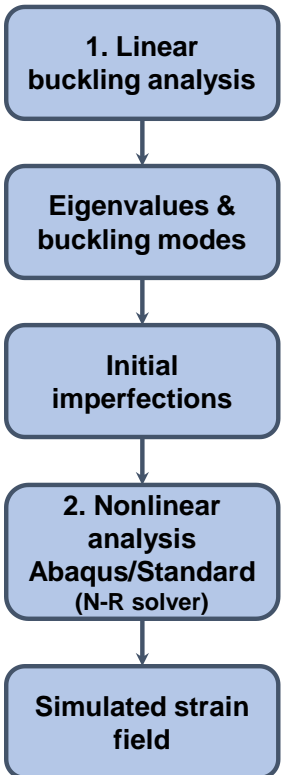
## 2. Digital twin development



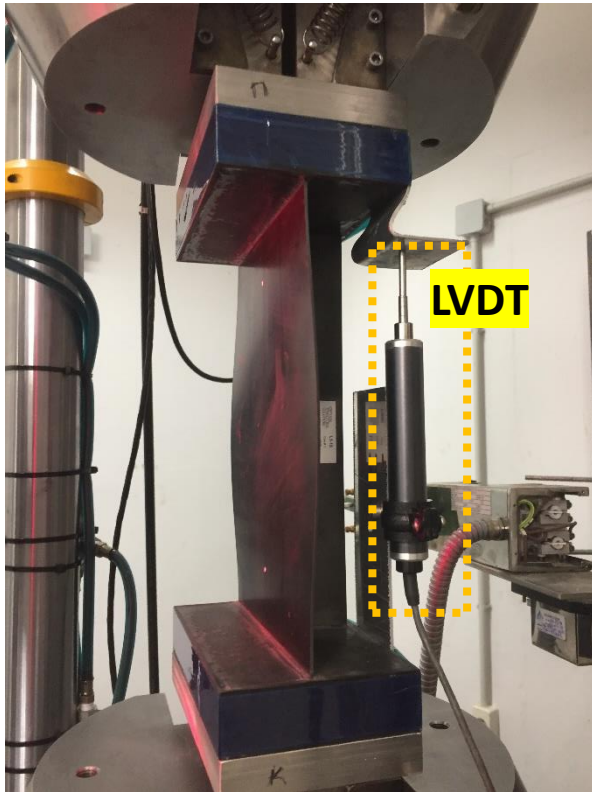
*Physical twin*



*Digital twin*



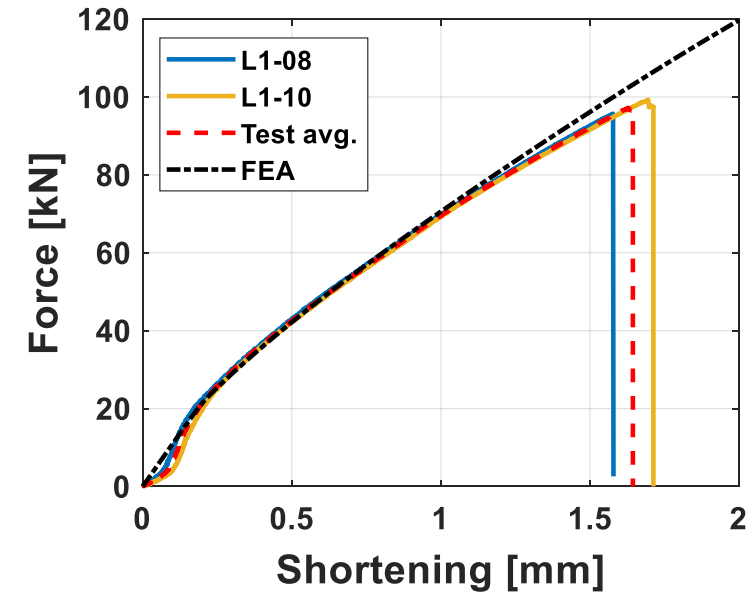
### 3. Experimental verification (1)



#### *Quasi-static uniaxial compression*

##### *test:*

- Displacement rate 0.5 mm/min
- Instron 8802 test machine with load capacity  $\pm 250$  kN
- LVDT for panel shortening measurements
- Buckling  $\sim 20.0$  kN
- Avg. collapse load 97.5 kN

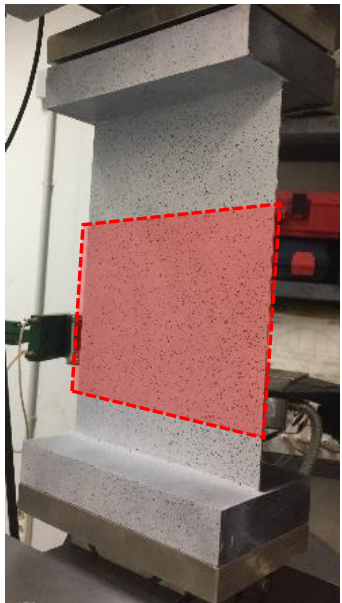


*Experimental and numerical  
force-shortening curves*

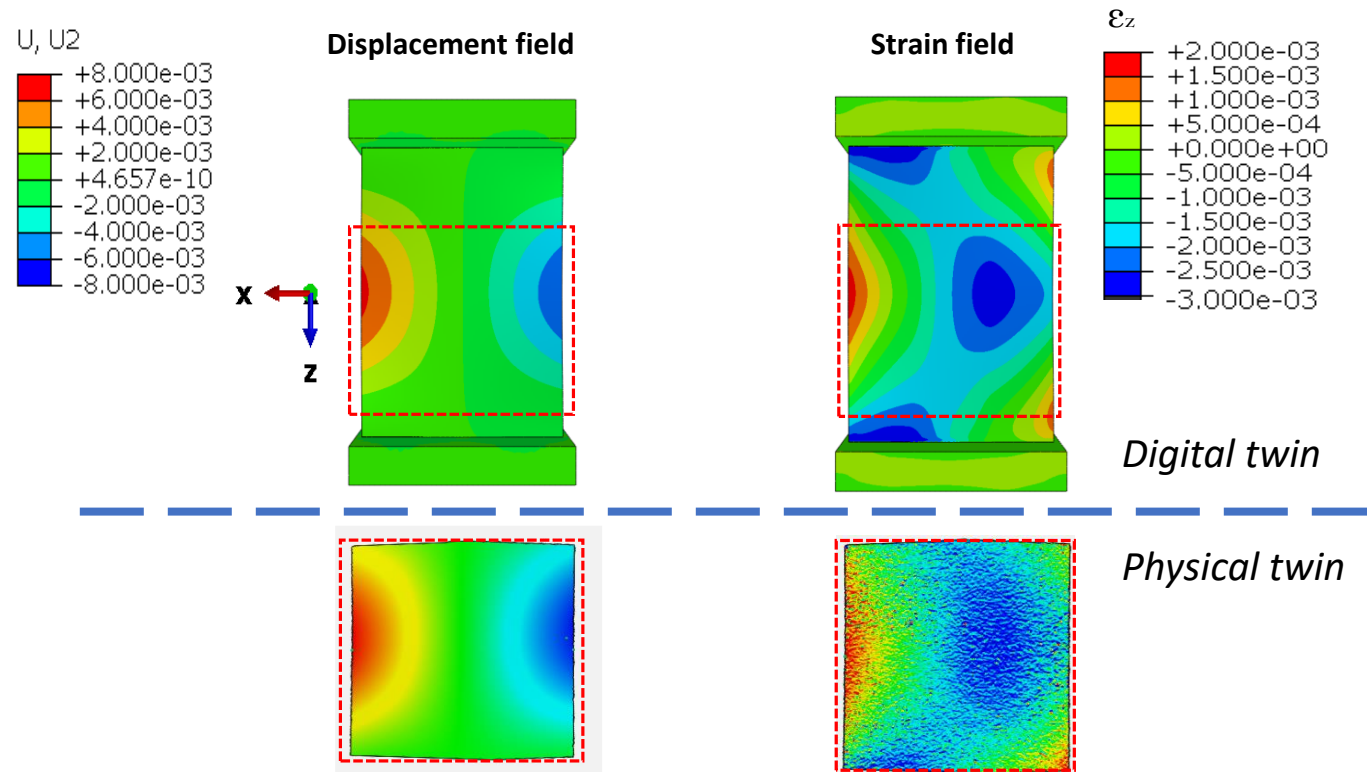
*Specimen response during  
post-buckling regime*

# 3. Experimental verification (2)

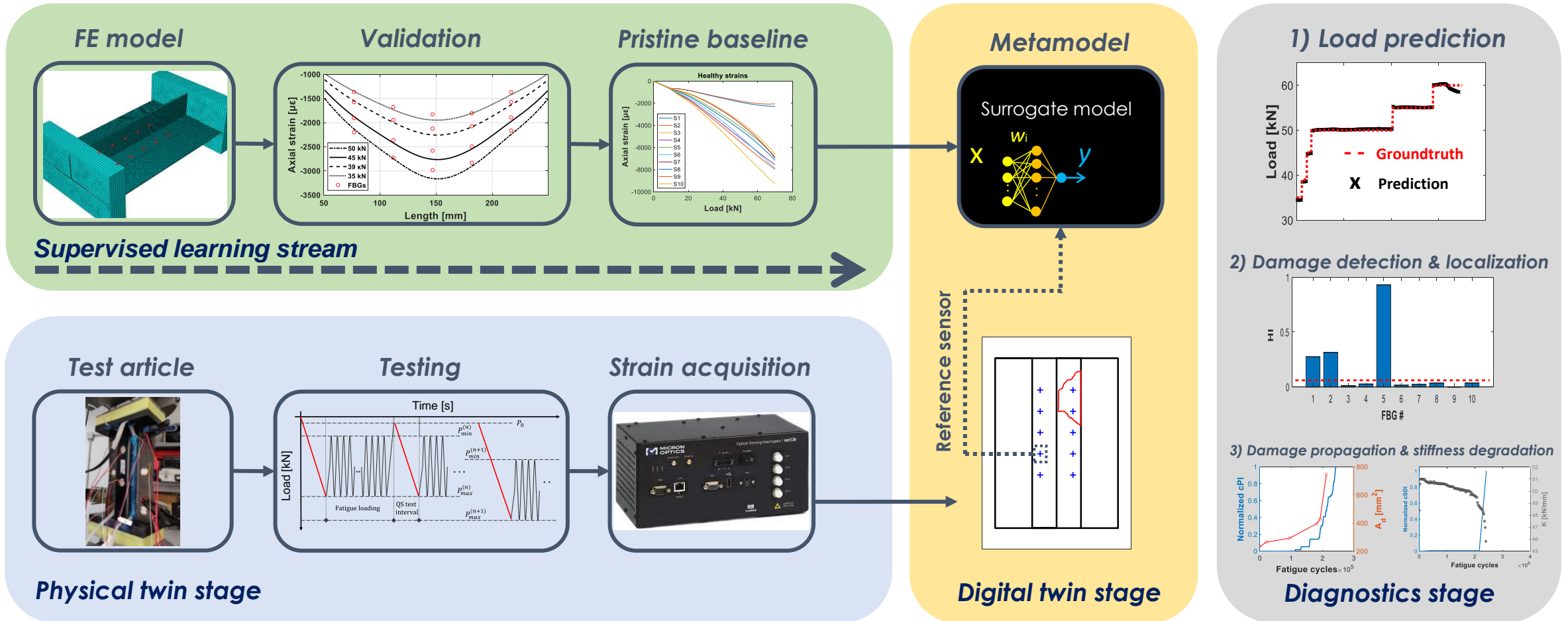
## Digital Image Correlation (DIC) measurements



Speckle pattern

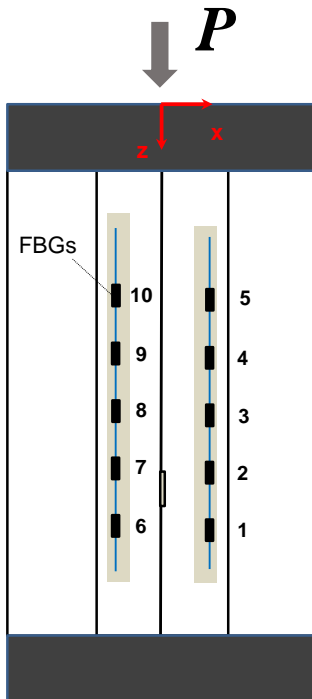


# 4. DT-based damage diagnosis



# 4.1 Surrogate modeling

A surrogate model is trained with input-output pairs provided by the DT.



1. Meta-model's variables:  $\mathcal{X} = \underbrace{\{x^{(i)}, z^{(i)}\}}_{\text{FBG spatial coordinates}}, \underbrace{P^{(i)}}_{\text{Load}}\}_{i=1}^N$

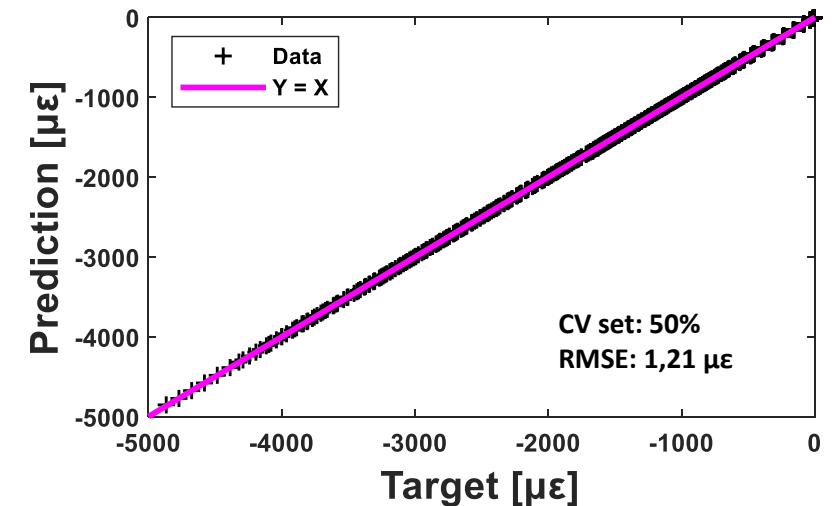
2. Radial Basis Function (RBF) surrogate:

$$\tilde{\mathcal{M}}(\mathcal{X}^{(j)}) = \sum_{i=1}^N w_i \psi(\|\mathcal{X}^{(j)} - \mathcal{X}^{(i)}\|) = y^{(j)}$$

- fixed basis:  $\psi(\rho) = \rho^3$

3. Learning dataset:  $\{\mathcal{X}^{(i)}; y^{(i)}\}, i=1, \dots, N$

- $N=1040$  strains, i.e., 100 loads  $P \in [0, 70]$  kN



*Accuracy of the trained surrogate model*



## 4.2 Strain-based feature extraction

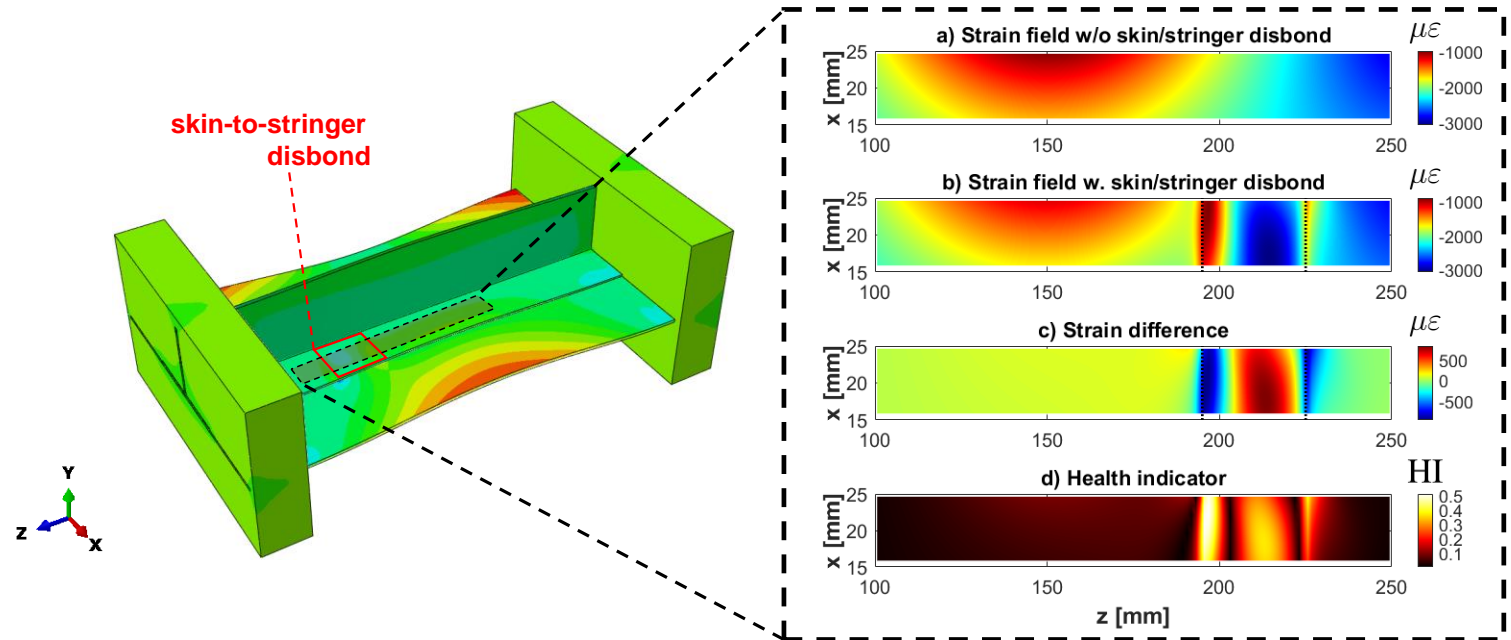
DT-based Health Indicator (HI):

$$HI_i = \left| \frac{\epsilon_{ref}^{(i)} - \epsilon_t^{(i)}}{\epsilon_{ref}^{(i)}} \right|$$

$i=1, \dots, 10$  : FBG label

$\epsilon_{ref}^{(i)}$  : DT's strain at the pristine state

$\epsilon_t^{(i)}$  : experimental strain during testing



*Strain modification in the vicinity of skin-to-stringer disbonds at -50 kN*

**Important:** HI strongly related to the boundary conditions, e.g., load.

## 4.3 Load identification

Load derives from the minimization of the following squared  $\ell^2$ -norm objective function  $F$ :

$$P = \operatorname{argmin}_P F(x^{(r)}, z^{(r)}, P) = \operatorname{argmin}_P \left\{ \|\tilde{\mathcal{M}}(x^{(r)}, z^{(r)}, P) - \mathbf{y}^m\|^2 \right\}$$

$\mathbf{y}^m$  : strain measurement by the reference FBG

Iterative estimation of  $P$  utilizing gradient descent:

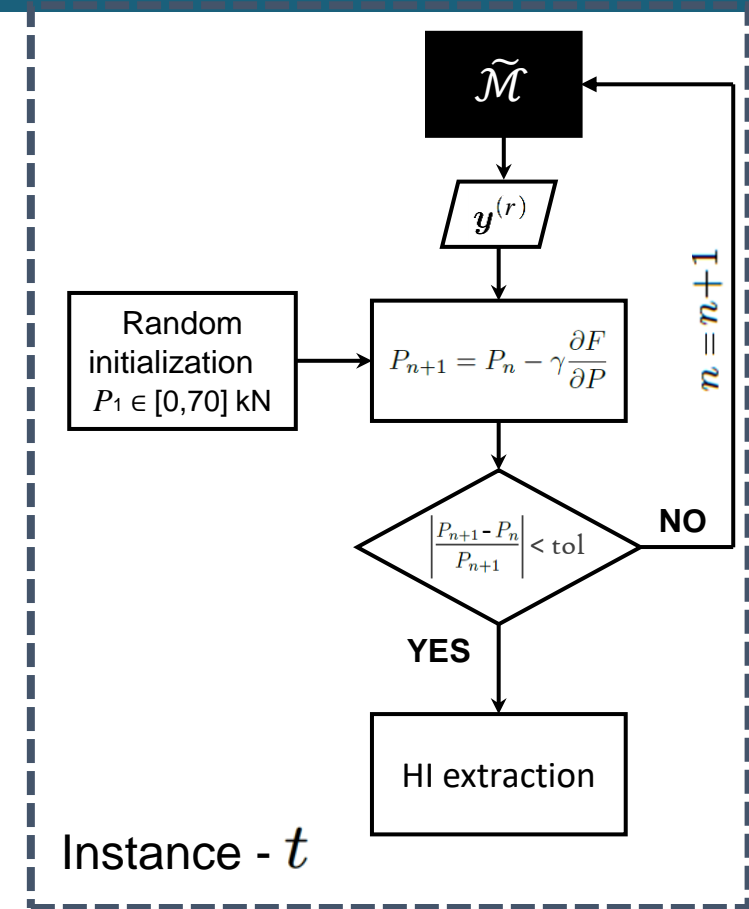
$$P_{n+1} = P_n - \gamma \frac{\partial F}{\partial P}, \quad \gamma : \text{step size}$$

Derivative term with central differences:

$$\frac{\partial F}{\partial P} = \frac{1}{\epsilon} \left[ \tilde{\mathcal{M}}(x, z, P) - \mathbf{y}^m \right] \cdot \left[ \tilde{\mathcal{M}}(x, z, P + \epsilon) - \tilde{\mathcal{M}}(x, z, P - \epsilon) \right]$$

$\epsilon$  : small perturbation

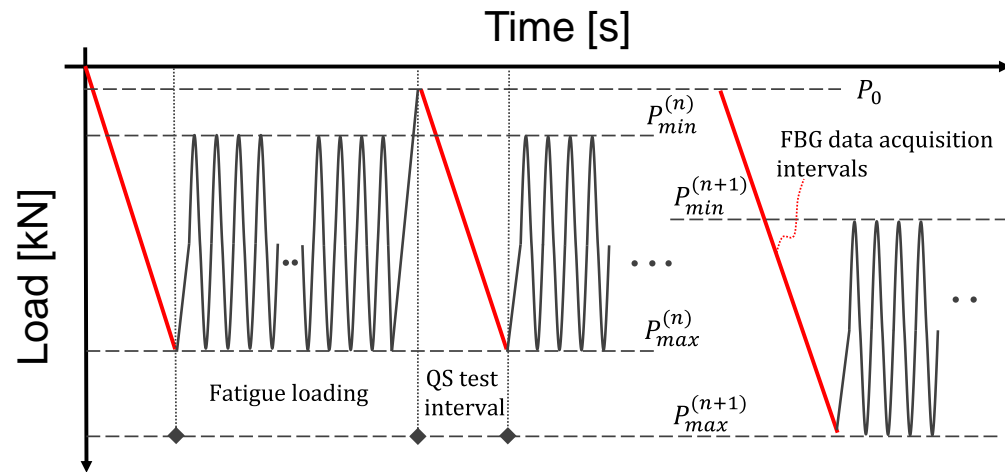
**Highlight:** Load is predicted by a sensor far from damage utilizing information from the pristine DT.



*Gradient-descent  
optimization algorithm*



# 5. Evaluation of the methodology



Test plan definition

- Block loading compression-compression fatigue
- FBG strains recorded during quasi-static test intervals every 500 cycles

## Details of the fatigue tests

SSP	Damage type	Damage location [x,z] (mm)	Initial damage area (mm) <sup>2</sup>	$P_{min}$ (kN)	$P_{max}$ (kN)	Consecutive cycles	Failure cycles
Panel #1	I - 10 J	[22.5,200]	1397.9	-4.0	-40.0	10,000	217,000
				-4.5	-45.0	177,000	
				-5.0	-50.0	30,000	
Panel #2	I - 7.4 J	[32.5,105]	232.5	-4.0	-40.0	10,000	243,000
				-4.5	-45.0	80,000	
				-5.0	-50.0	90,000	
				-5.5	-55.0	63,000	

# 5.1 Multi-level diagnosis

## I. Damage detection and localization

$$DI_i = \begin{cases} 1, & \text{if } HI_i > \text{threshold} \\ 0, & \text{if } HI_i \leq \text{threshold} \end{cases}$$

## II. Damage type identification (boxplot statistics)

### a) Type 1: Damage propagation

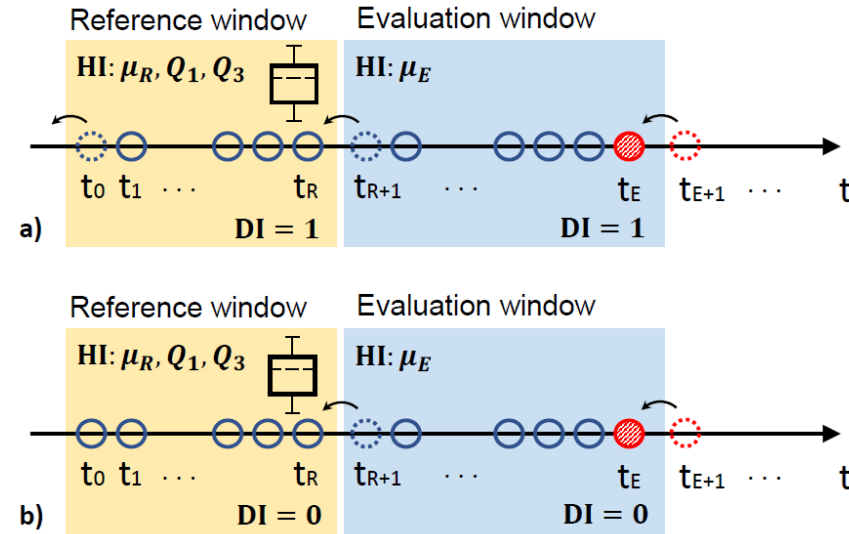
$$PI_i(t_E) = \begin{cases} 1, & \text{if } \mu_E > Q_3 + 1.5(Q_3 - Q_1) \\ & \text{or } \mu_E < Q_1 - 1.5(Q_3 - Q_1) \\ 0, & \text{otherwise} \end{cases}$$

### b) Type 2: Stiffness degradation

$$SDI_i(t_E) = \begin{cases} 1, & \text{if } \mu_E > Q_3 + 1.5(Q_3 - Q_1) \\ & \text{or } \mu_E < Q_1 - 1.5(Q_3 - Q_1) \\ 0, & \text{otherwise} \end{cases}$$

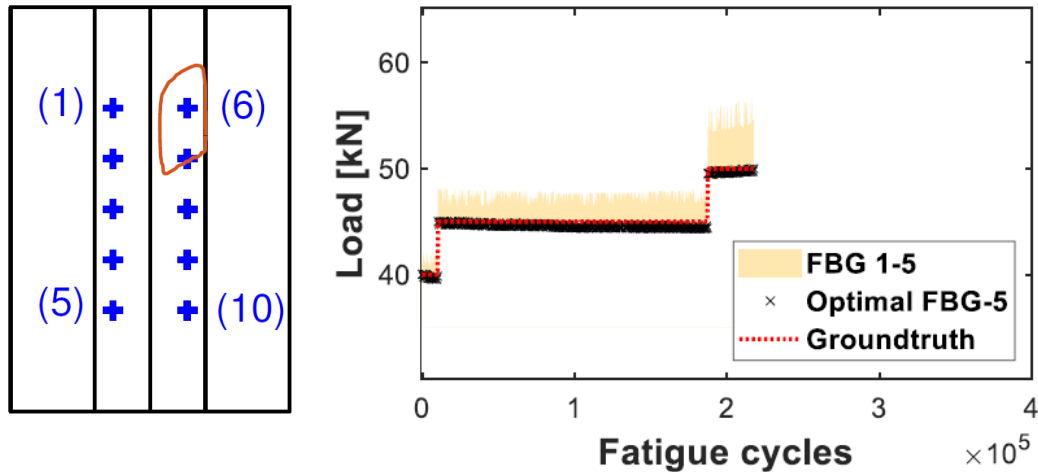
a) Sensors detecting local damage (DI=1) evaluate potential propagation

b) Sensors not detecting local damage (DI=0) evaluate potential stiffness degradation (global effect)

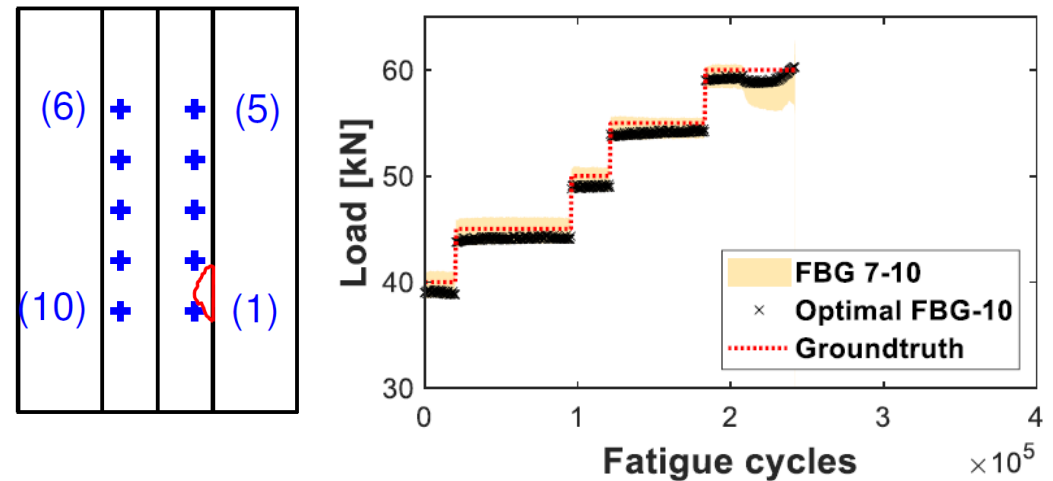


# 6. Results: Load predictions

Impacted panel #1



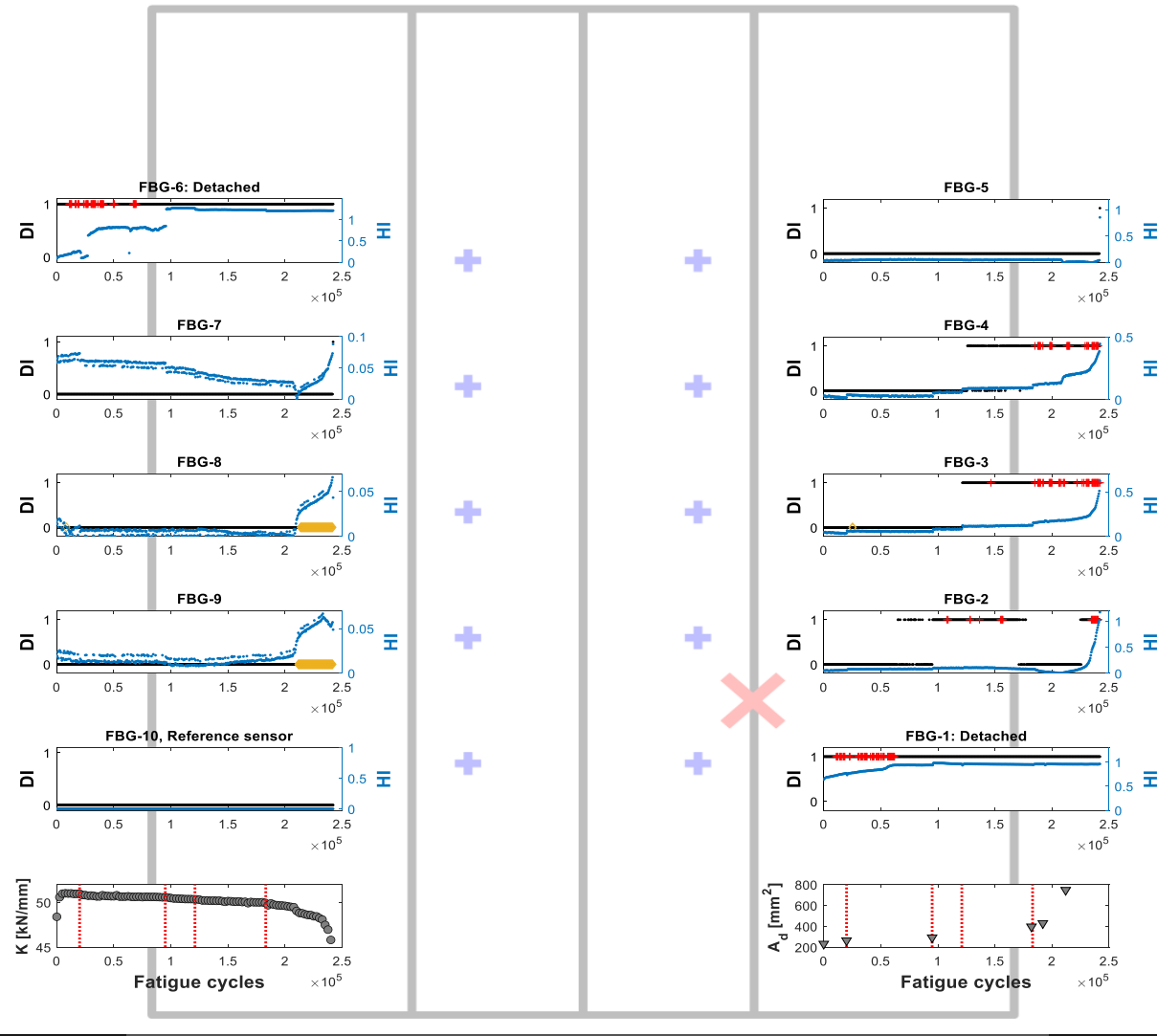
Impacted panel #2



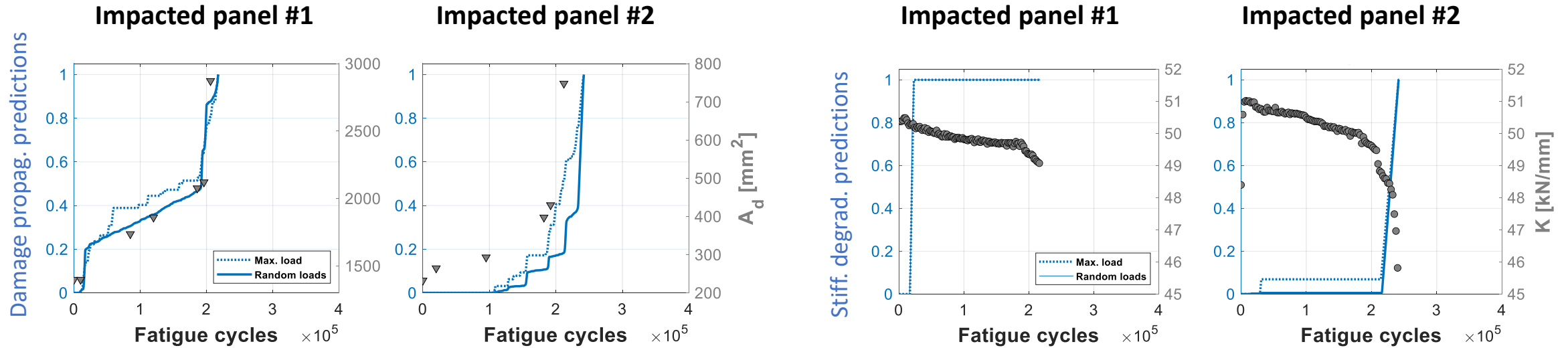
- Groundtruth loads reflect to the maximum load during each quasi-static test.

# 6. Results: Multi-level diagnostics

Impacted panel #2



# 6. Results: Cumulative predictions



$A_d$ : Damaged area (measured with DolphiCam)

K: Experimentally measured stiffness

# Concluding remarks

1. A structural DT of a pristine single-stringer composite panel was efficiently established in terms of a verified finite element model
2. Exploitation of a RBF surrogate model, trained with deterministic strain data from the finite element model, enabled the DT-based damage diagnosis concept
3. Damage diagnosis was realized with a strain correlation between the DT's and corresponding static strains extracted from the actual specimen via permanently affixed FBGs
4. Damage-unaaffected FBGs were effectively utilized as load evaluators by iteratively estimating the load with a gradient descent optimization algorithm
5. The proposed methodology revealed the presence of a skin-to-stringer disbond and monitored the forthcoming fatigue disbond growth

# CASE STUDY II:

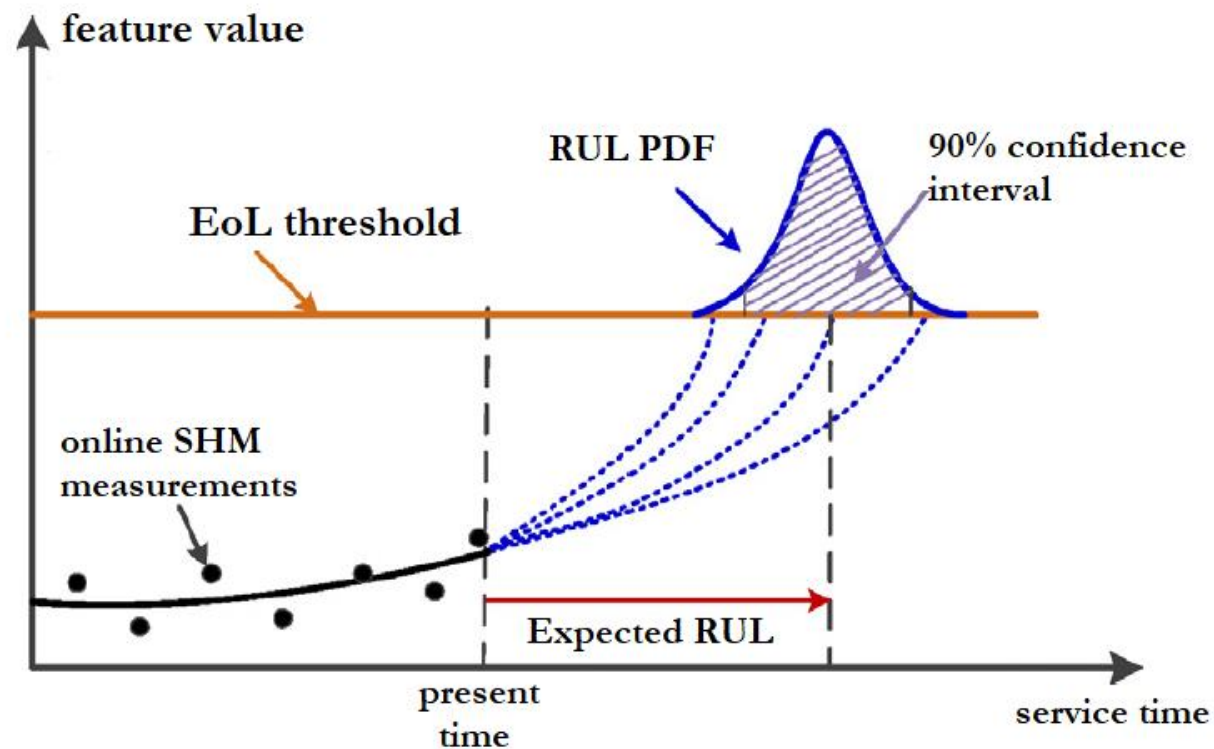
## Remaining Useful Life Prognostics in complex structures

## *Prognosis (prɒɡnɒʊsɪs)*

A **prognosis** is an estimate of the future, a forecast, foreknowledge (in Greek)

Central concept:      **RUL** = Remaining Useful Life

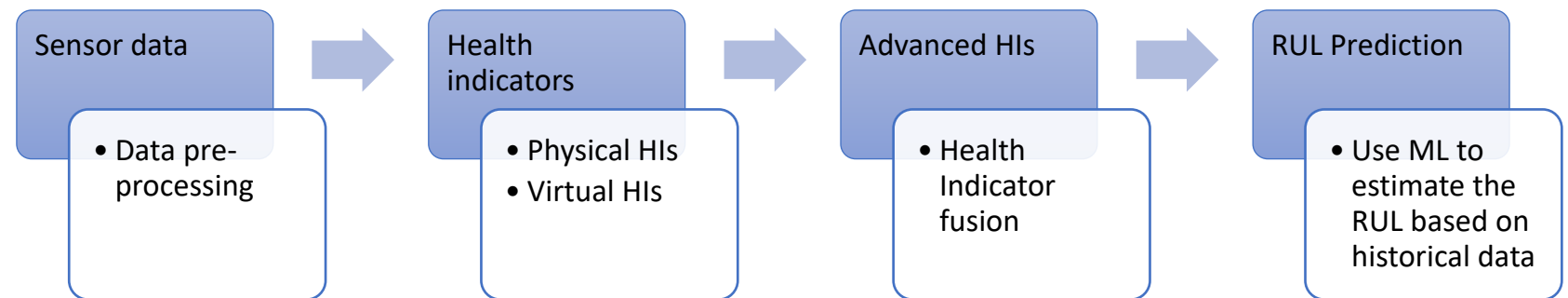
SHM data-driven  
prognosis





# Problem Statement: RUL prediction

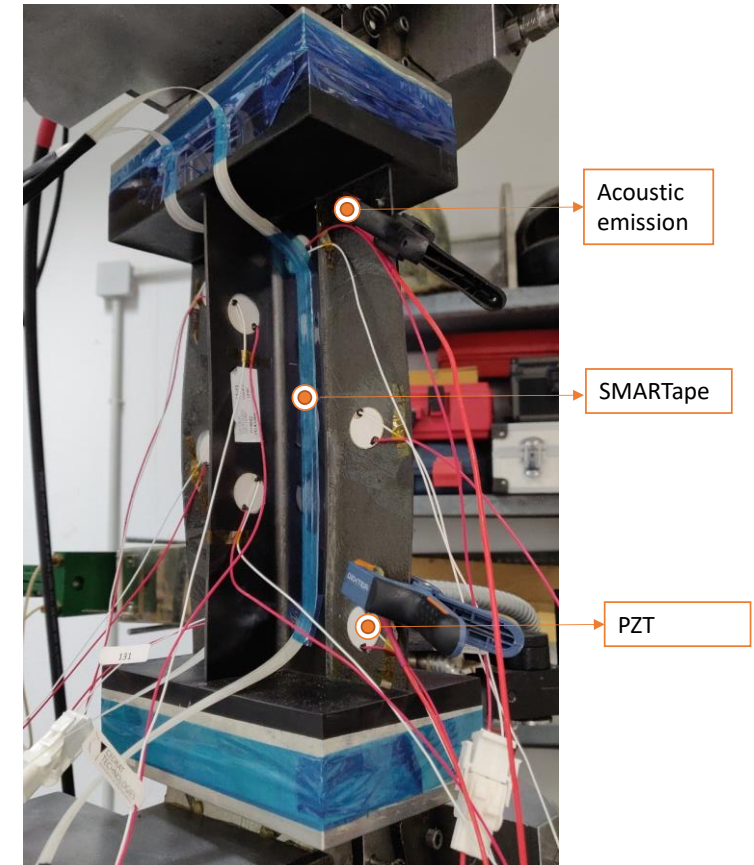
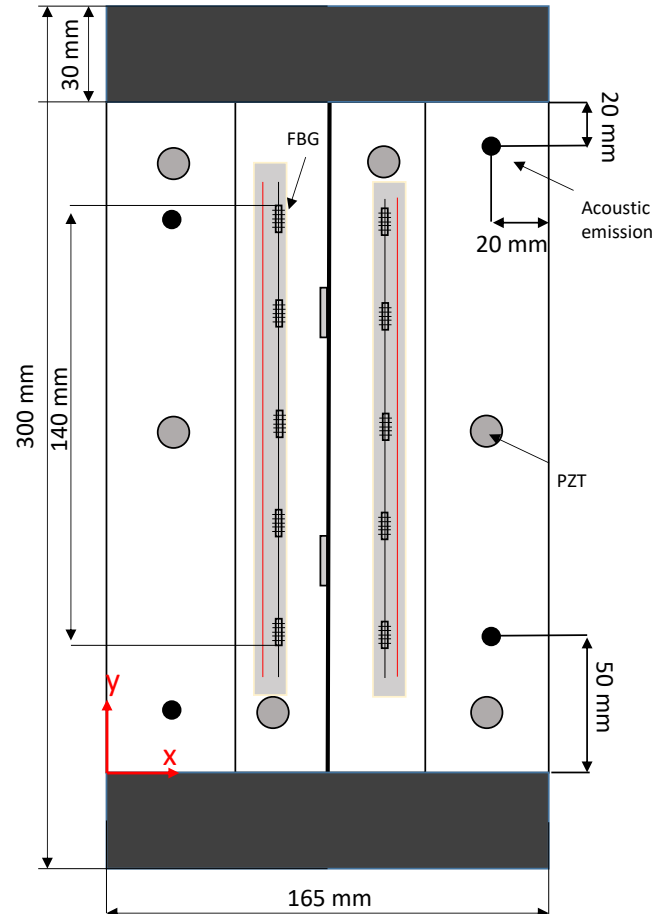
- **Data-driven prognostics** require historical data to train ML models to predict the RUL
- The **accuracy of the prediction** is dependent on the degradation features (**Health Indicators - HIs**)
- **Key attributes**
  - ❖ **Monotonicity**
  - ❖ **Prognosability**



Generic Methodology

# Experimental Campaign(1): Panel geometry

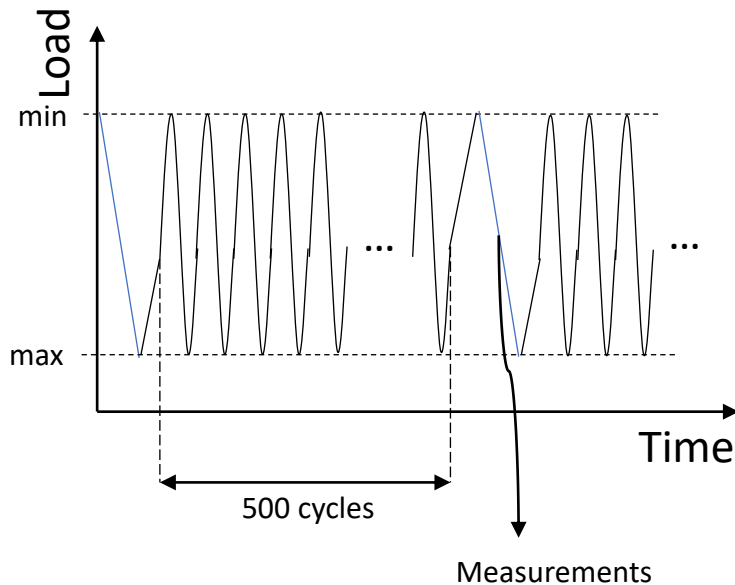
- **Single T-shaped Stiffened Panels**
- Layup:
  - Skin:  $[45/-45/0/45/90/-45/0]_S$
  - Stiffener:  $[45/-45/0/45/-45]_S$
- Dimension:
  - 300x165x1.85 mm<sup>3</sup> (Nominal)
  - 240x165x1.85 mm<sup>3</sup> (Free length)
- Sensors:
  - **FBG strain sensors**
  - Acoustic emission sensors
  - PZT lamb wave sensors



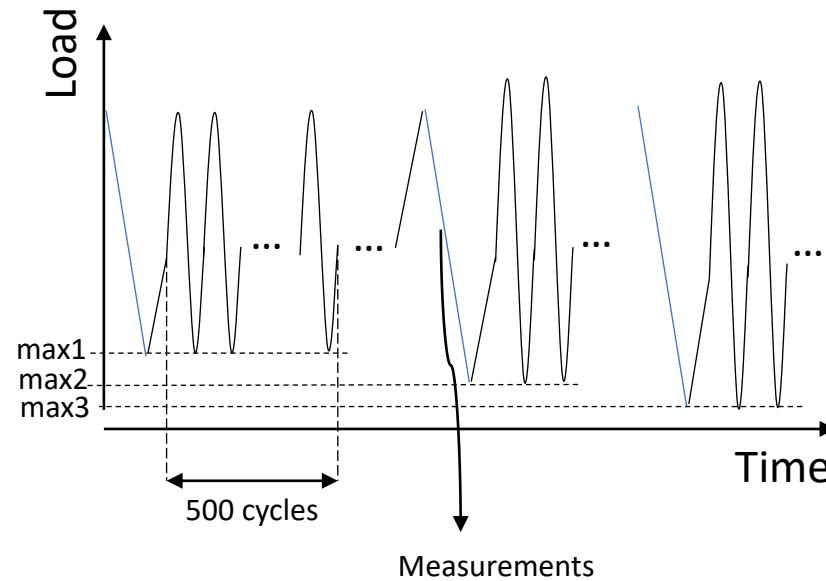
# Experimental Campaign(2): Fatigue experiments – Raw strain data

- 3 different fatigue scenarios were investigated with increased loading complexity:

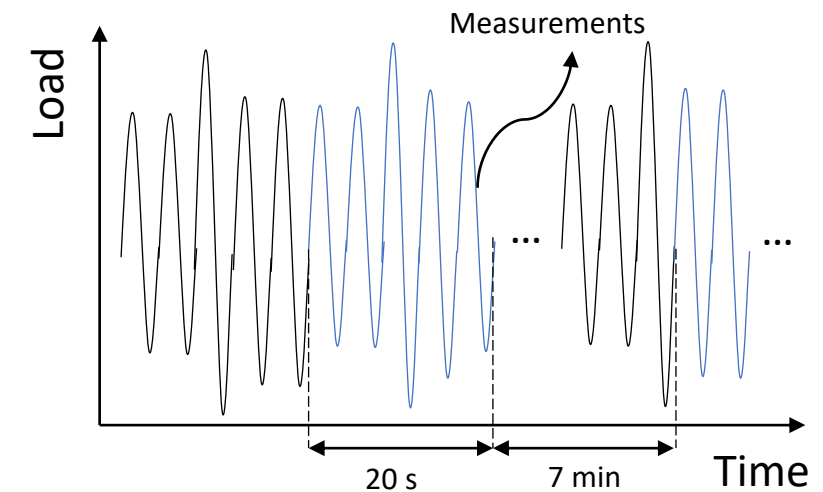
Constant Amplitude Fatigue



Variable Amplitude Fatigue



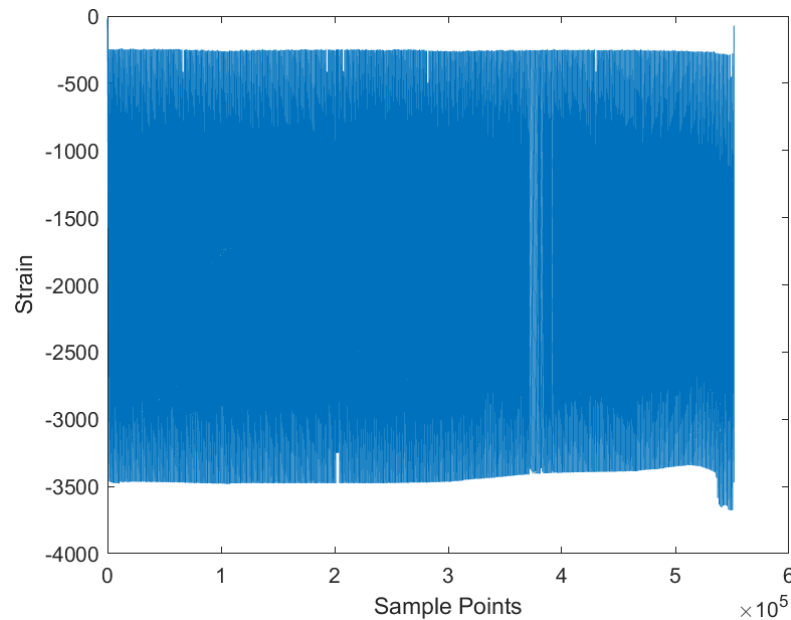
Random Amplitude Fatigue (spectrum)



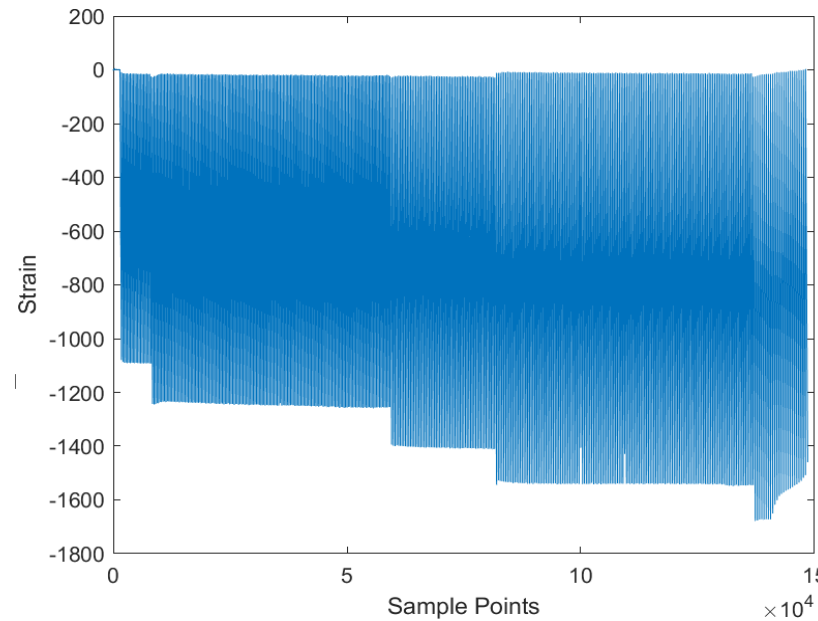
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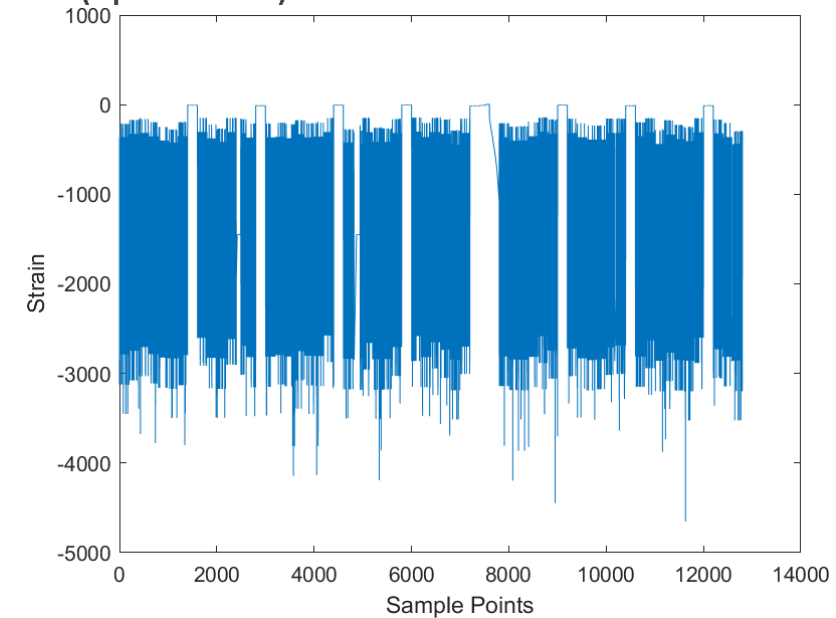
Constant Amplitude Fatigue



Variable Amplitude Fatigue



Random Amplitude Fatigue  
(spectrum)



# Health Indicators(1): Physical HIs

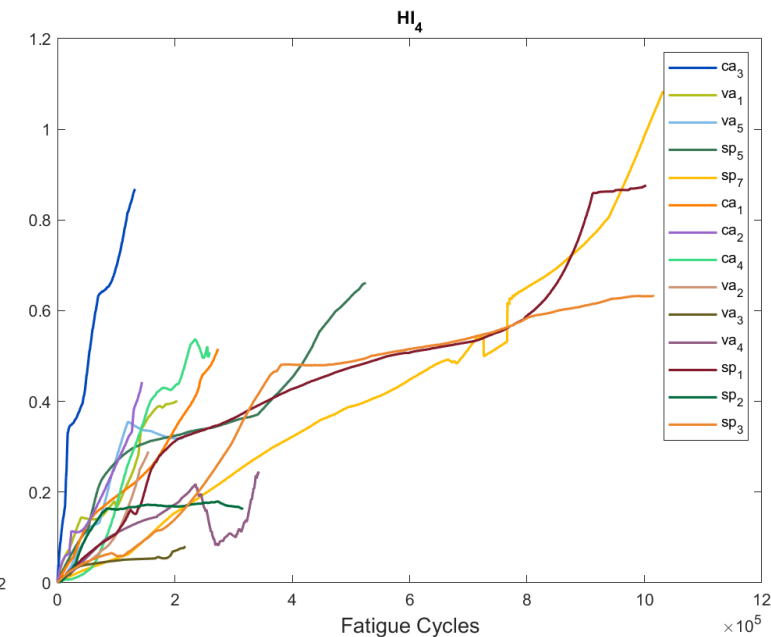
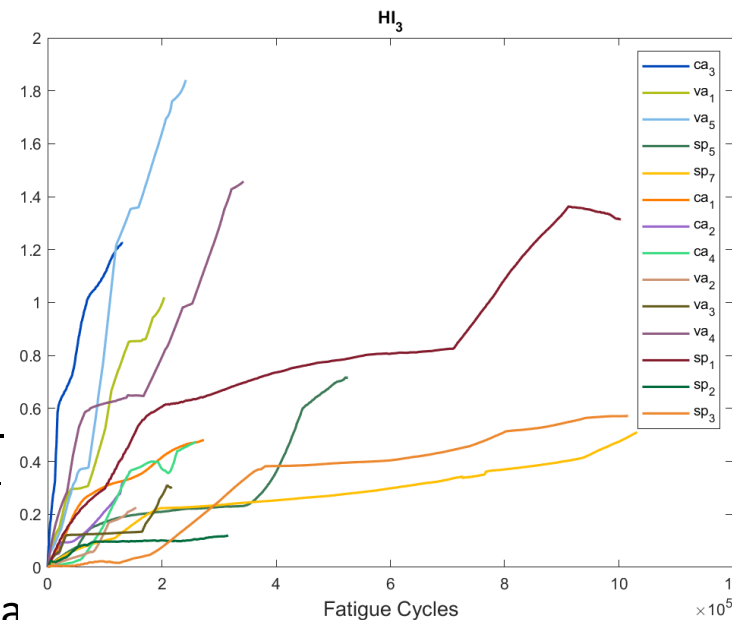
- HIs correlated to physical measurements
- Extracted from simple expressions on strain data

$$HI_3(t) = \sqrt{\sum_{i=1}^N \left| 1 - \frac{\varepsilon^i(t)}{\varepsilon_{ref}^i} \right|^2}$$

$$HI_4(t) = \sqrt{\sum_{i=1}^N \left( HI_2^i(t) \right)^2},$$

$$\text{Where } HI_2^i(t) = \frac{\varepsilon^i(t)}{\frac{1}{n} \sum_1^n \varepsilon^i(t)} - \frac{\varepsilon^i(t=0)}{\frac{\sum_1^n \varepsilon^i(t=0)}{n}}$$

n=1,...,5 number of sensor at each foot a...  
N=1,...,10 total number of sensors



# Health Indicators(2): virtual HI

- HIs not directly correlated to physical measurements
- PCA based feature extraction

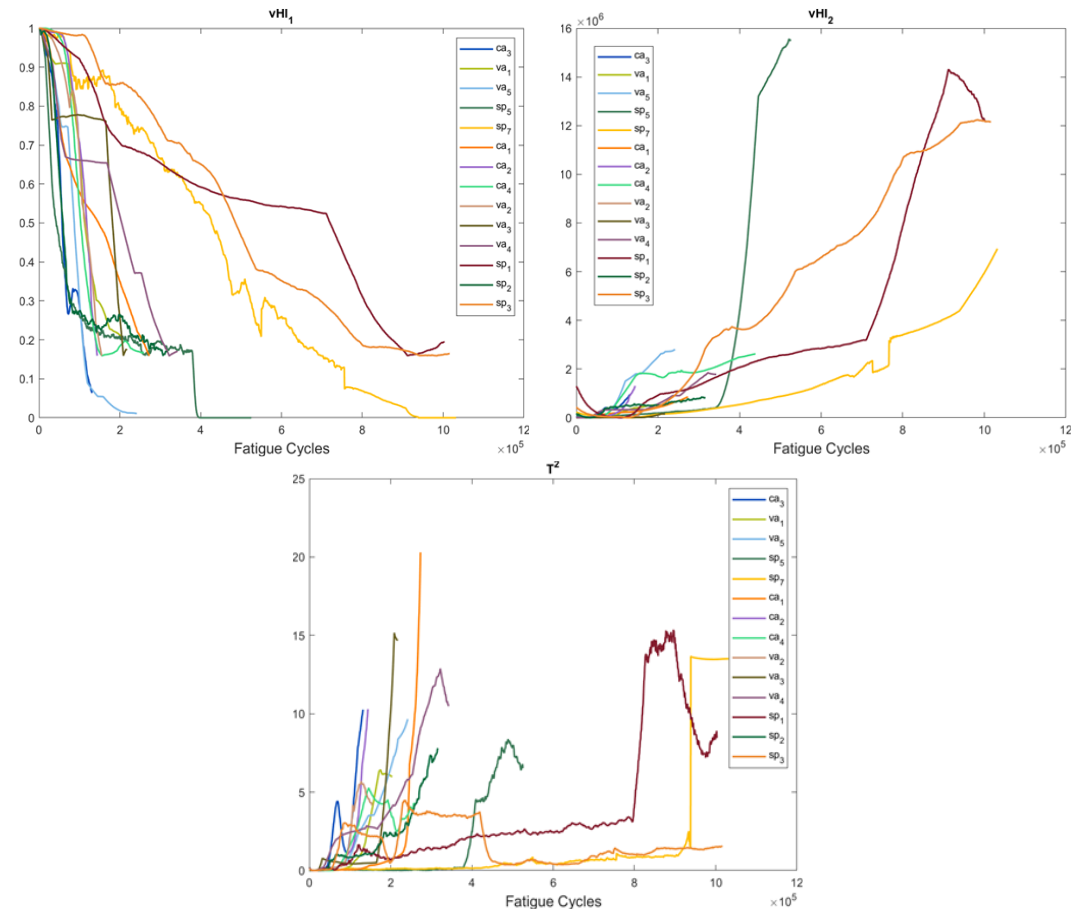
$$vHI_1 = \exp\left(-\frac{(d_L - d_{Lmin})^2}{\sigma_L}\right),$$

Where,  $\sigma_L = -\frac{(d_{Lmax} - d_{Lmin})^2}{2} \left[ \frac{1}{\log_{10}\epsilon} + \frac{1}{\log_{10}(\epsilon + \delta)} \right]$  and  $\epsilon = \delta = 0.01$

SPC metrics \*

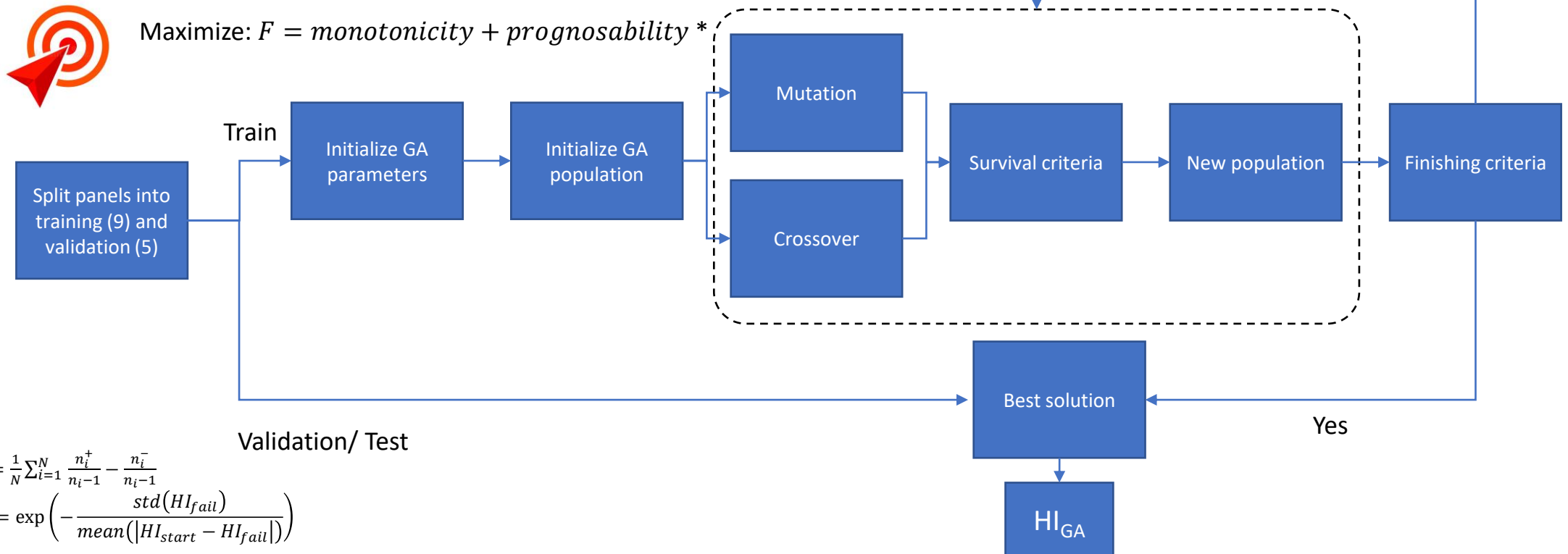
$$vHI_2(t) = Q = \sum_1^N (x_i(t) - x_{ri}(t))^2,$$

$$T^2(t) = \sum_1^N \frac{\tau_i^2(t)}{\lambda_i}$$



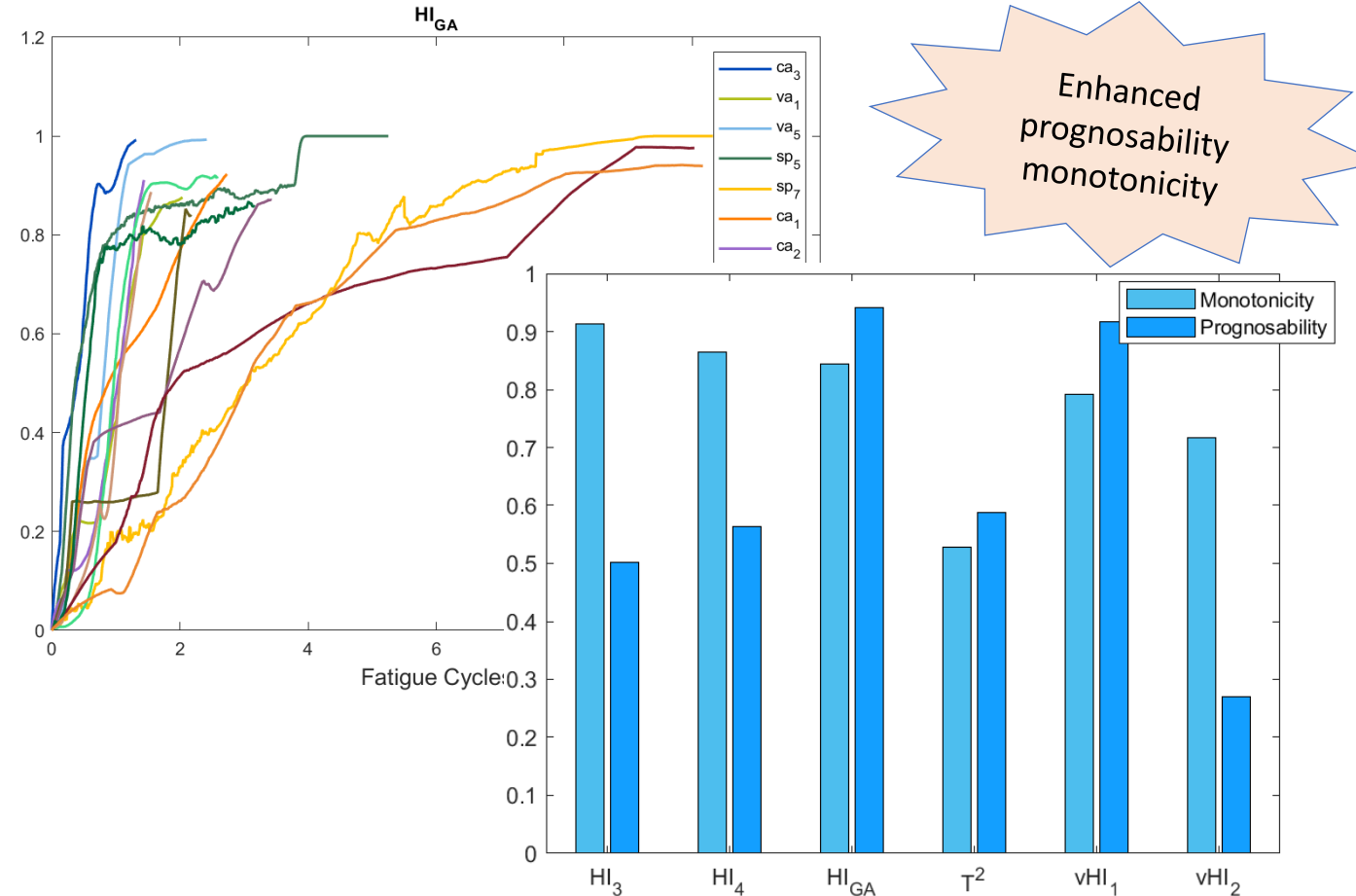
# Health Indicator fusion(1)

- Genetic Algorithms are utilized to fuse the HIs:



# Health Indicator Fusion(2)

- *Accepted solution:*
- $HI_{GA} = vHI_1 \left( vHI_2 - \frac{HI_4 + 0.5HI_5}{HI_4} \right) - 1$
- Repeatability (50 runs):
- - average monotonicity:  $0.90 \pm 0.026$
- - average prognosability:  $0.96 \pm 0.024$





# RUL predictions (1): Procedure

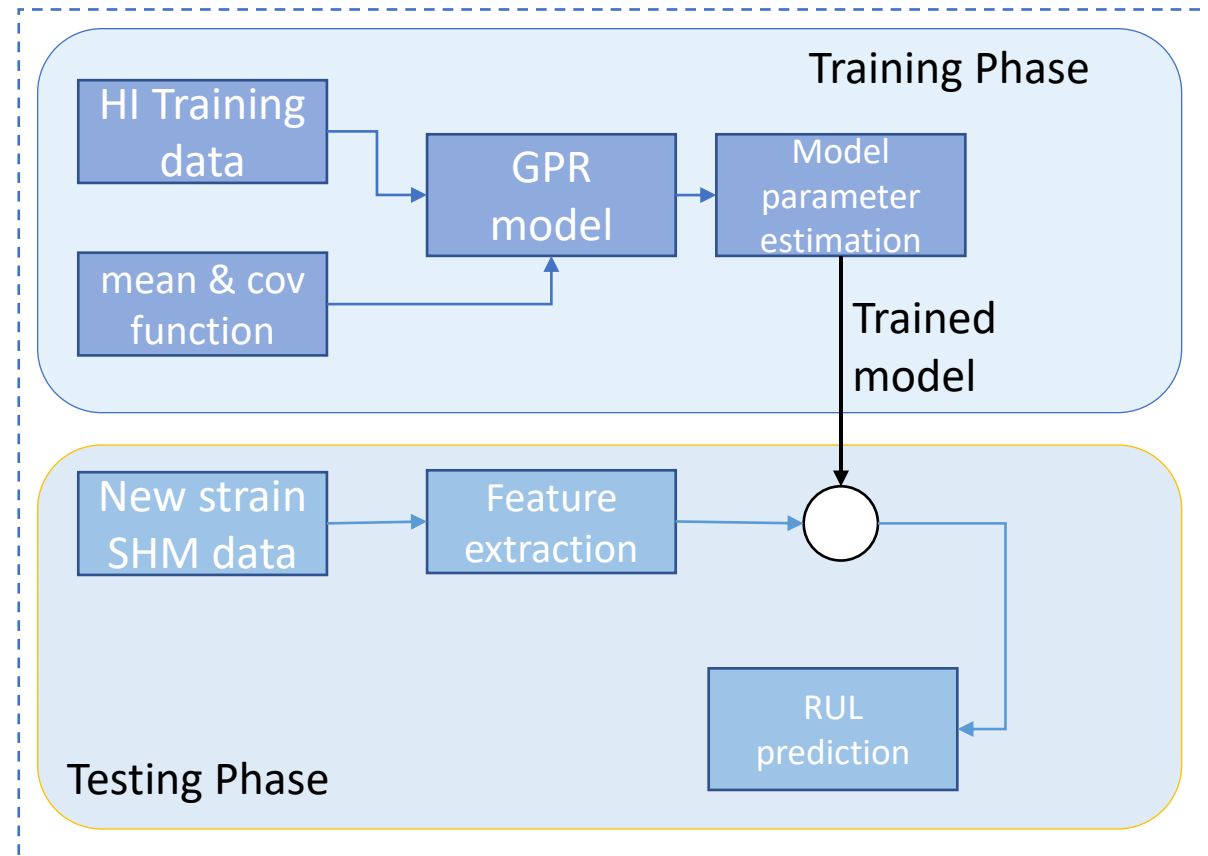
- Gaussian Process regression was used for the RUL estimation task
- 1 panel from the test set was used to tune the GP parameters:

❖ Linear mean function:

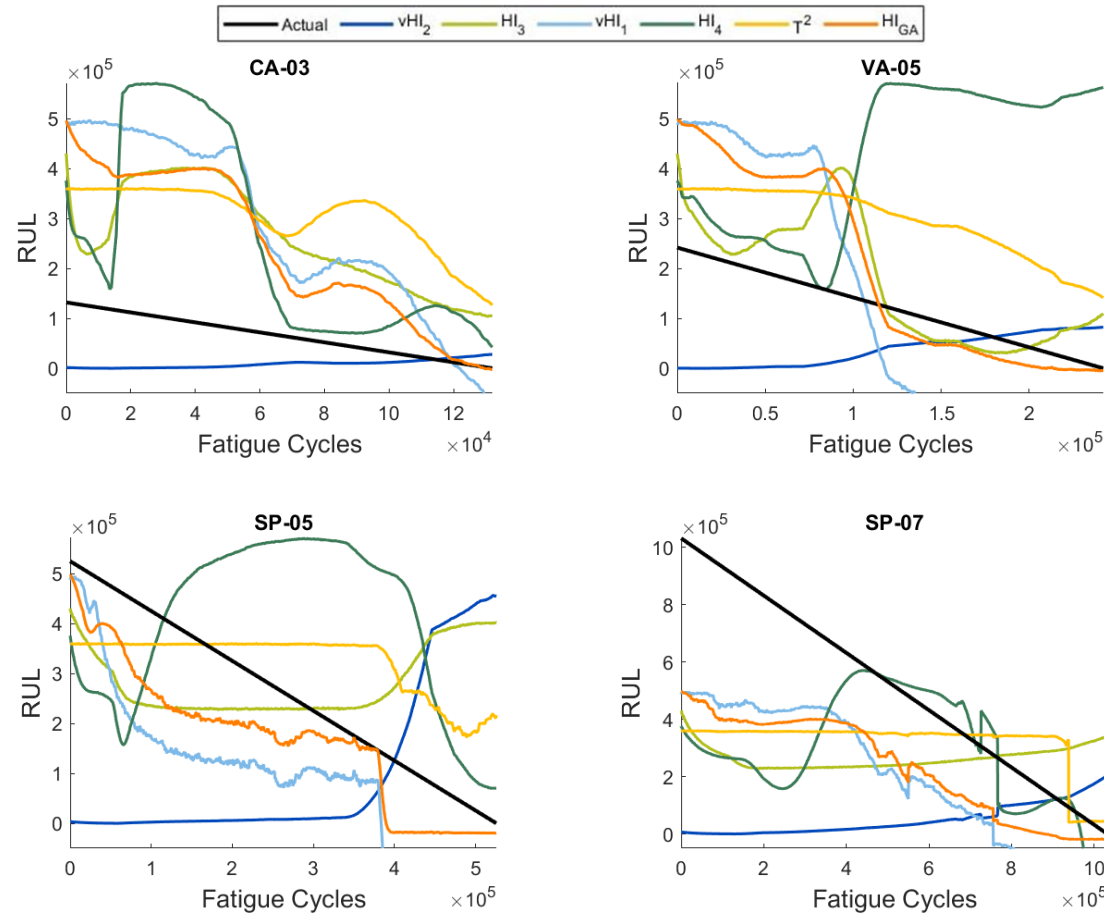
$$m(x) = ax + b$$

❖ Matern 5/2 covariance function:

$$k(r) = \sigma_f^2 \left( 1 + \frac{\sqrt{5}r}{\sigma_l} + \frac{5r^2}{3\sigma_l^2} \right) \exp\left(-\frac{\sqrt{5}r}{\sigma_l}\right)$$



# RUL predictions(2): Results

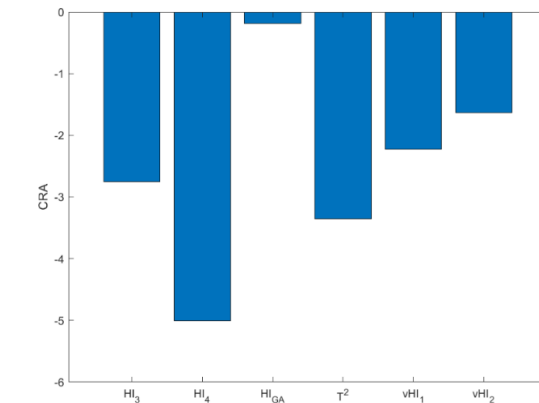
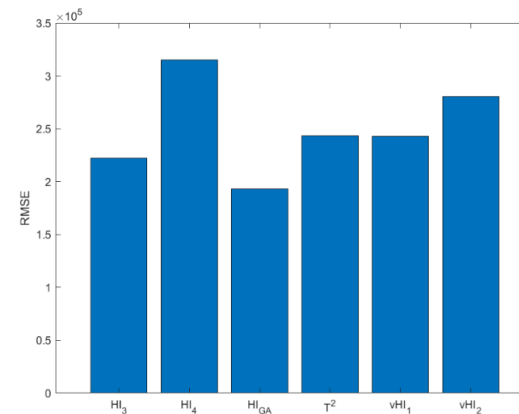
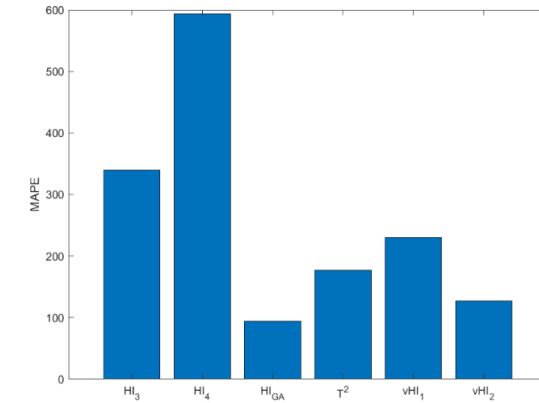
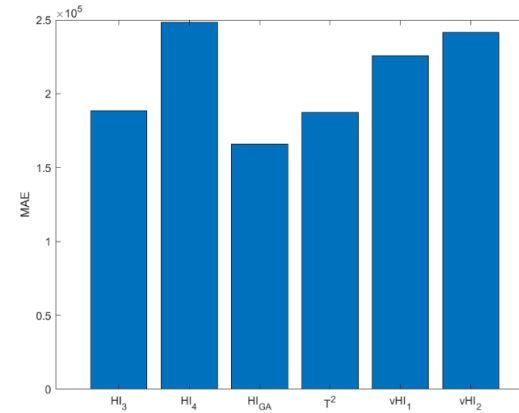


- $HI_{GA}$  converges to the true RUL in all cases
- $vHI_1$  shows the second best predictions
- $HI_3$  shows poor performance for SP panels
- $HI_4$  shows good performance only for CA-03
- $T^2$  in most cases does not converge to the true RUL
- $vHI_2$  shows the worst performance, incapable of converging to the true RUL

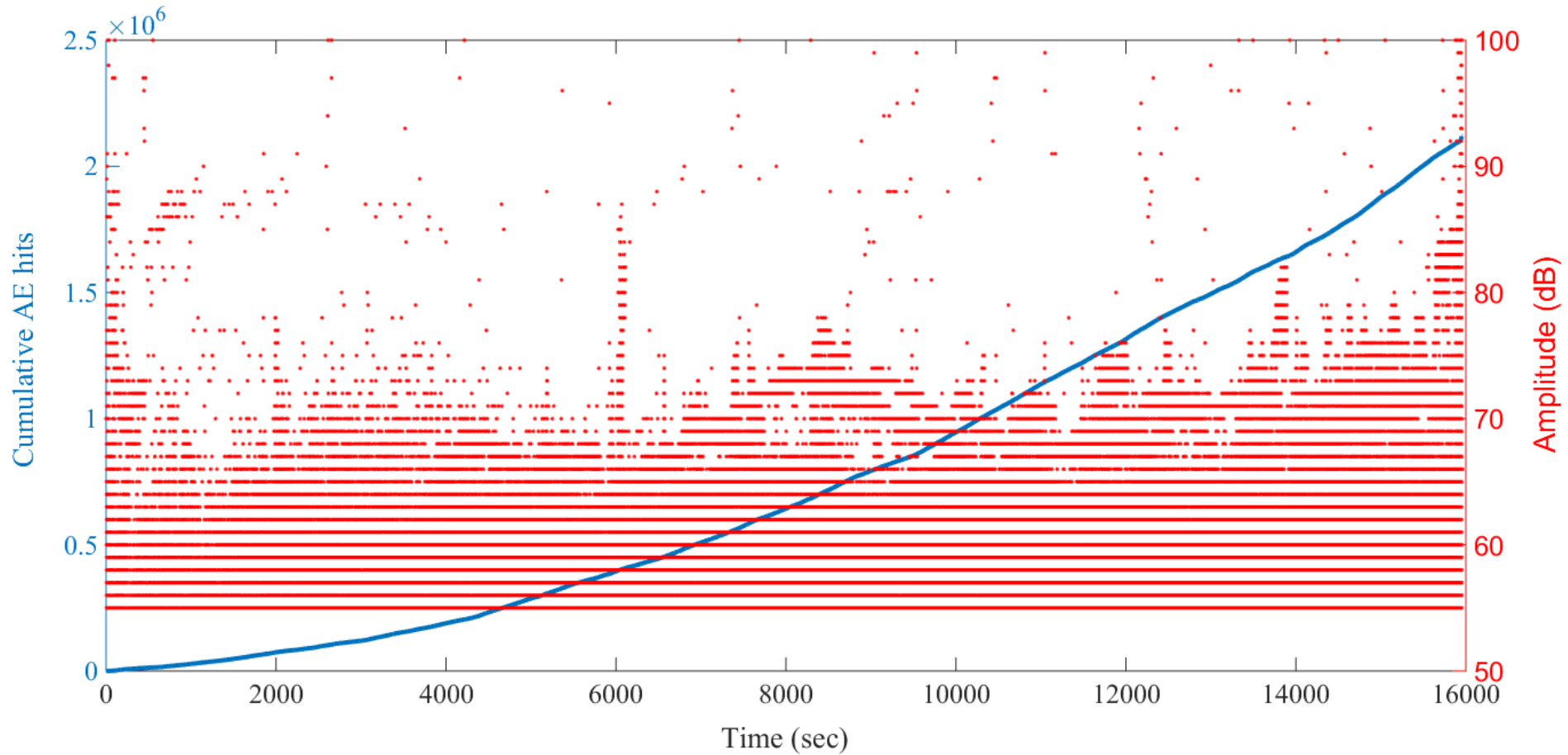
# RUL prediction: Performance metrics

- Classical metrics were employed to validate the prognostic performance
  - Mean Absolute Error (MAE)
  - Mean Absolute Percent Error (MAPE)
  - Root Mean Squared Error (RMSE)
  - Cumulative Relative Accuracy (CRA)

$HI_{GA}$   
outperforms  
in every  
metric

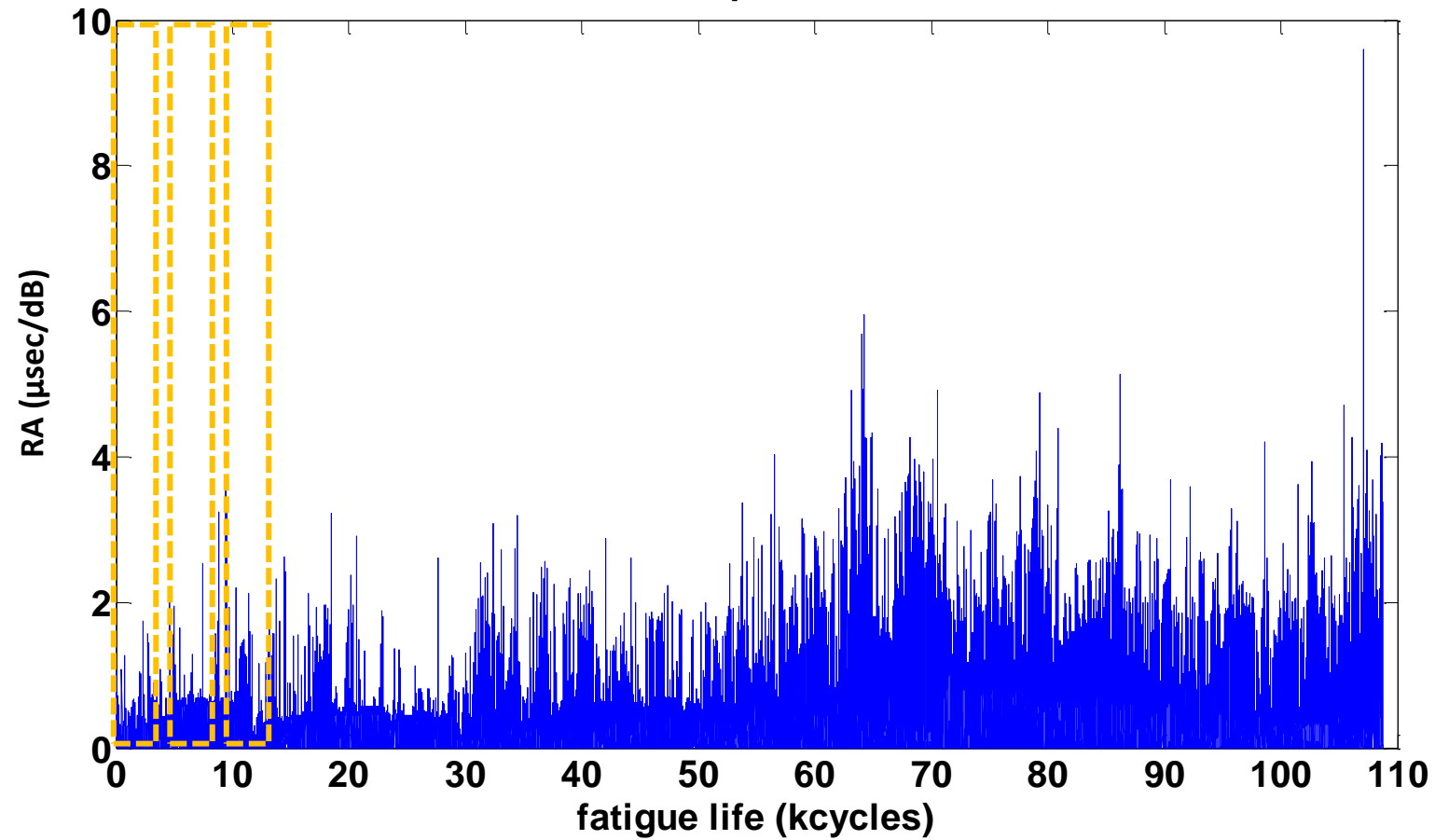


# AE raw data



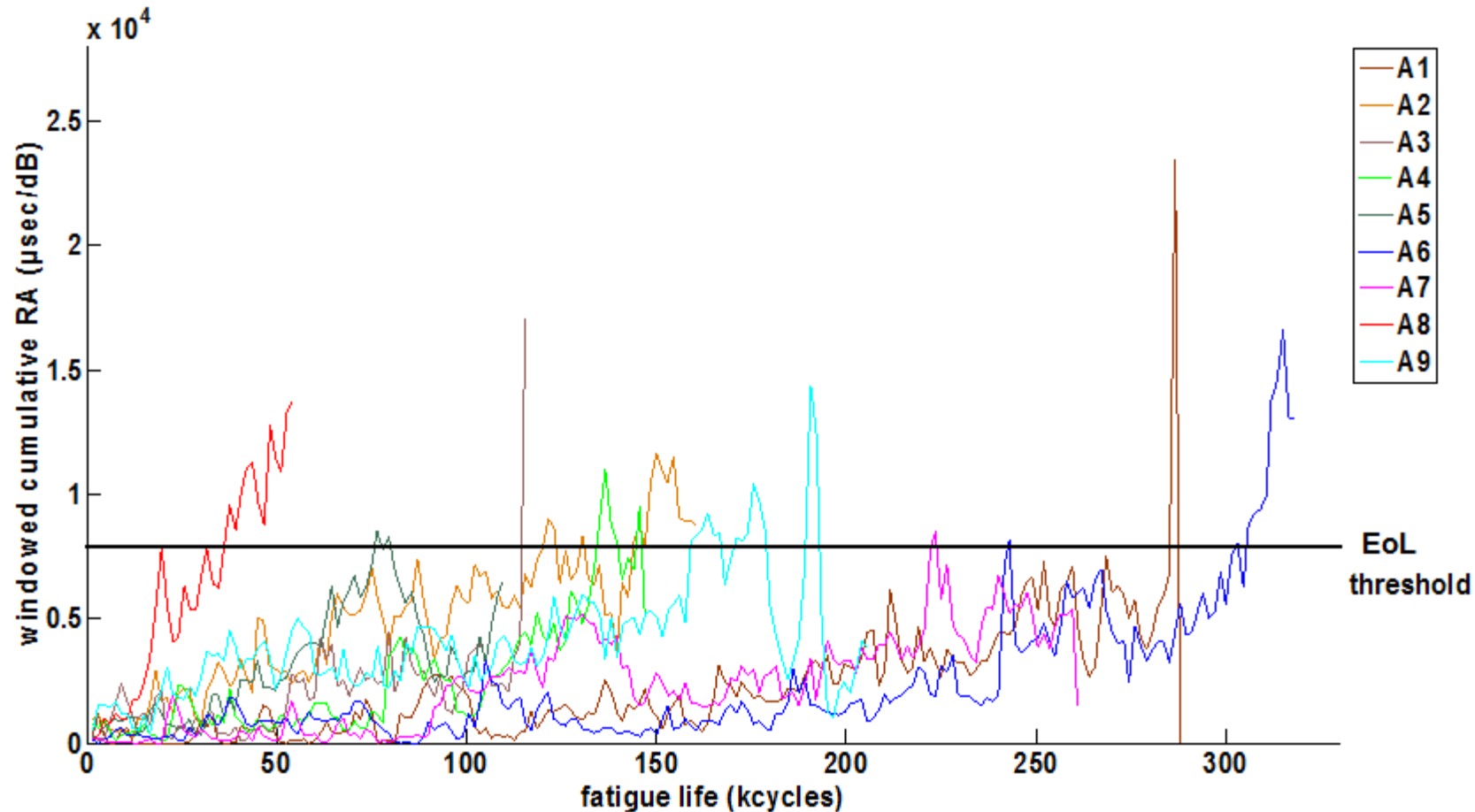
*~2,2 million AE hits!!  
Too many and not periodically distributed*

Coupon A5



A windowed CRA (cumulative risetime/amplitude) feature is calculated in periodic windows of 2.5 minutes or 1500 cycles

# Resulted degradation histories



*A few tens or hundreds points each degradation history!!  
EoL threshold needed – final state has to be unique*

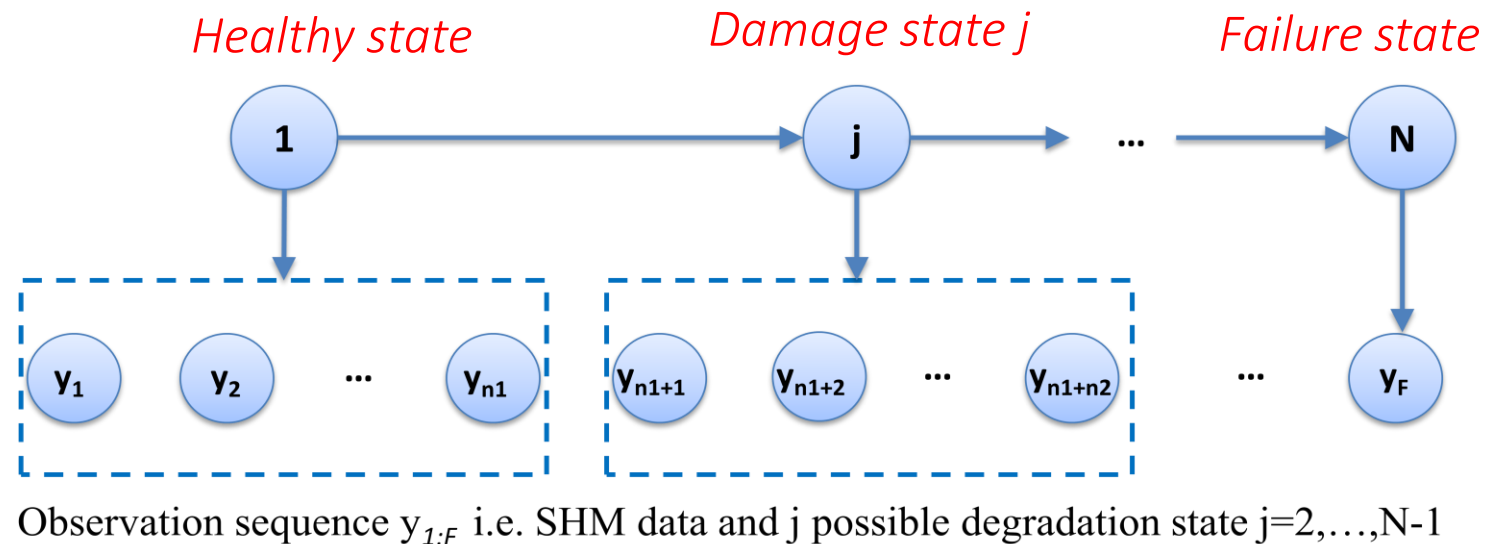
# Algorithms for RUL prediction

- ML/AI algorithms (Neural Networks, Gaussian processes, Gradient Boosting etc)
- Statistical models (Hidden Semi-Markov models, Proportional Hazards model etc)

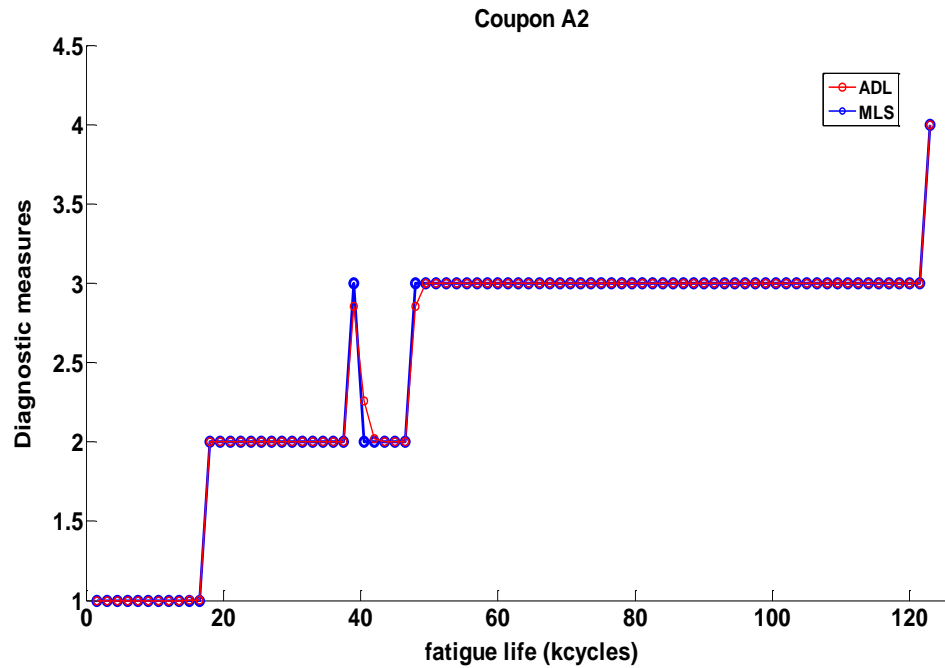


# Focus: Hidden State Semi Markov model

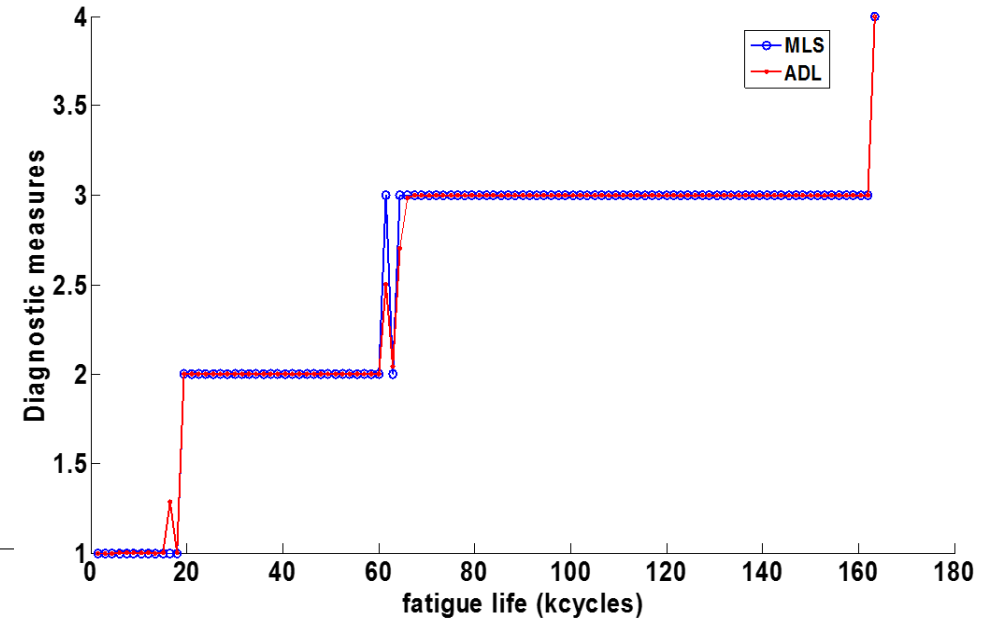
- ✓ *Damage evolution in composites is modeled as a doubly stochastic hidden Markov process that manifests itself via structural health monitoring (SHM) observations*
- ✓ *NHHSMM (an extension of the Hidden semi-Markov Models to account for non-homogeneity i.e. age dependence in state transitions) is utilized to model damage progression*



# Diagnostics – Health state identification



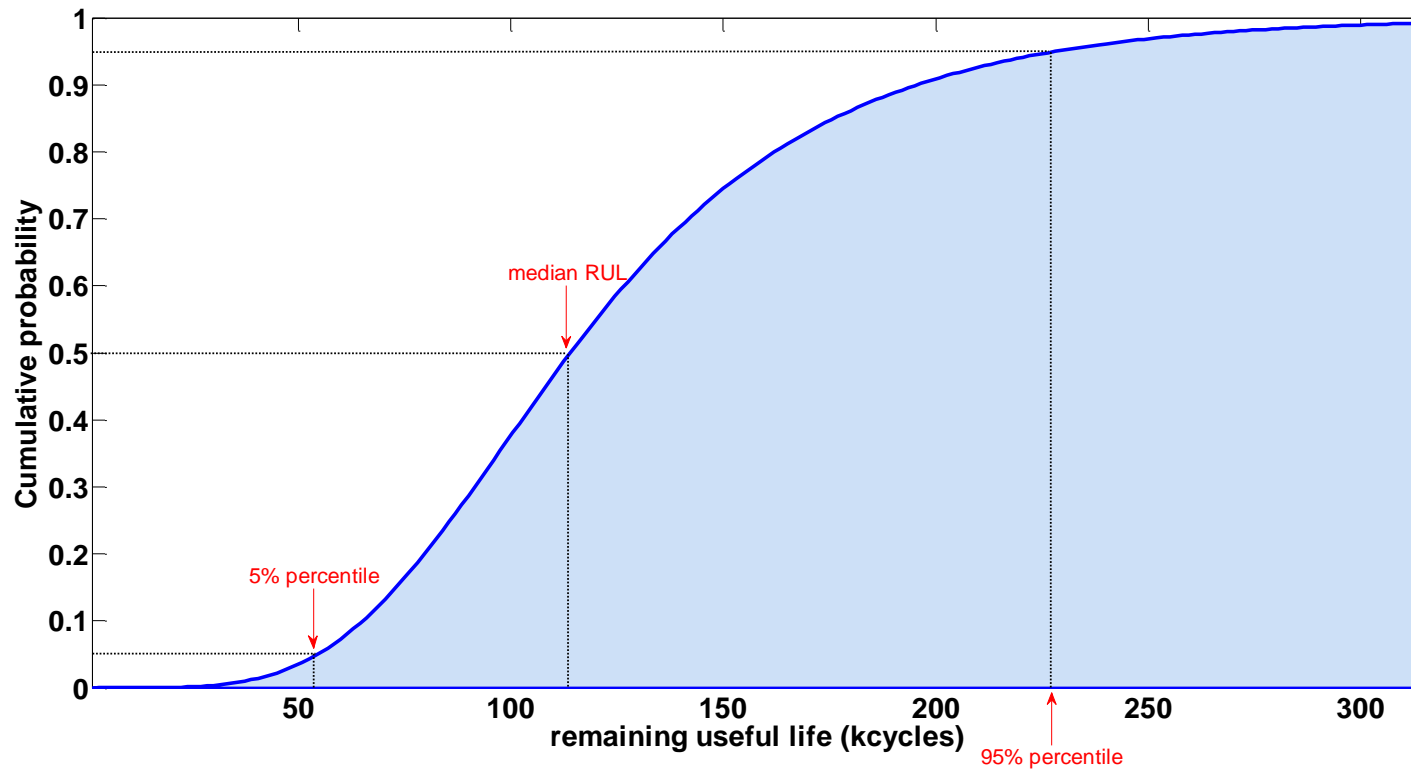
ADL and MLS for coupon A2



ADL and MLS for coupon A9

A real time 3-D visualization tool such as X-ray CT would be required in order to monitor in detail the developed damage mechanisms and their synergies and determine to what extent of damage these health states correspond to.

# Prognostic results – probabilistic aspect



Cumulative distribution function for RUL at  $t_p=1.5$  kcycles of coupon A9

**The target** in prognostics is the estimation of the conditional (on SHM data) reliability and finally the Remaining Useful Life (RUL) of the system.

- Reliability function:

$$R(t | y_{1:t_p}, L > t_p, \mathbf{M}) = \Pr(L > t | y_{1:t_p}, L > t_p, \mathbf{M})$$

- The CDF and mean of RUL:

$$\Pr(RUL_{t_p} \leq t | y_{1:t_p}, \mathbf{M}) = 1 - R(t + t_p | y_{1:t_p}, \mathbf{M})$$

$$\widehat{RUL}(t | y_{1:t_p}, L > t_p, \mathbf{M}) = \int_0^\infty R(t + \tau | y_{1:t_p}, L > t_p, \mathbf{M}) d\tau$$

# Focus - Bayesian Neural Networks

An alternative machine learning approach handles the RUL estimation as a nonlinear regression task mathematically described as:

$$y(\mathbf{x}) = RUL(\mathbf{x}) = f(\mathbf{x}, \boldsymbol{\theta}) + e$$

Where  $\mathbf{w}$  the network weight and bias parameters

$$p(\mathbf{w}|\mathbf{D}) \sim p(\mathbf{D}|\mathbf{w})p(\mathbf{w})$$

$$p(\mathbf{D}|\mathbf{w}) = \prod_{i=1}^N p(y_i|\mathbf{x}_i, \mathbf{w}) = \prod_{i=1}^N (2\pi/b)^{-\frac{1}{2}} \exp \left[ -\frac{b}{2} \{y_i - f(\mathbf{x}_i, \mathbf{w})\}^2 \right]$$

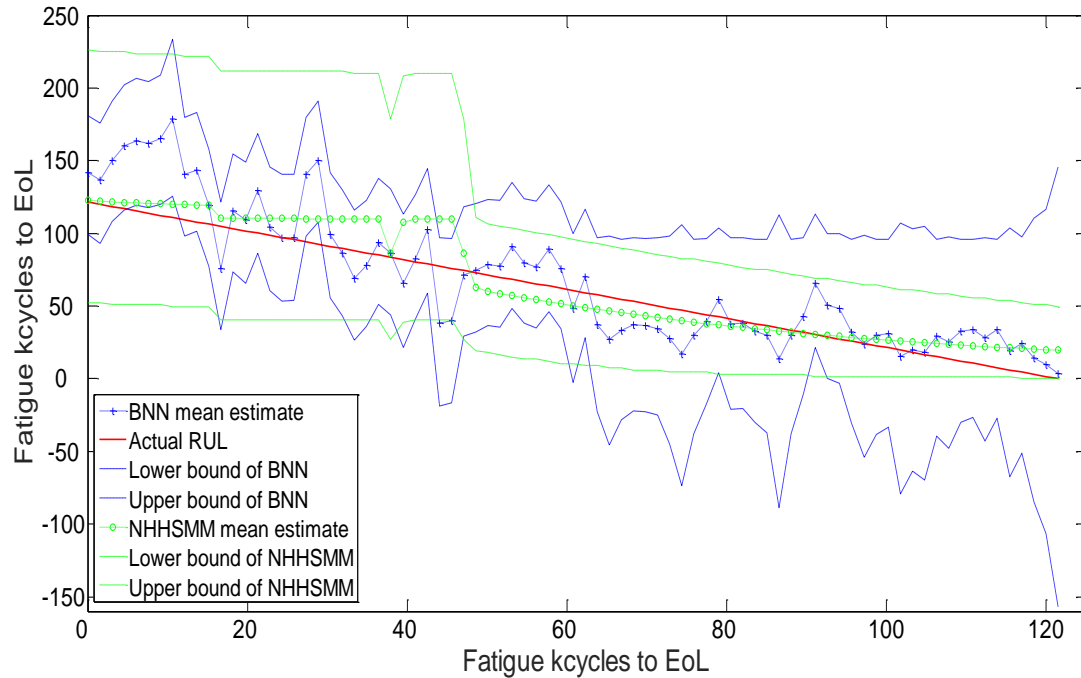
$$p(y_{new}|\mathbf{x}_{new}, \mathbf{D}, a, b) = \int p(y_{new}|\mathbf{x}_{new}, \mathbf{w}, b) p(\mathbf{w}|\mathbf{D}, a, b) d\mathbf{w}$$

MCMC

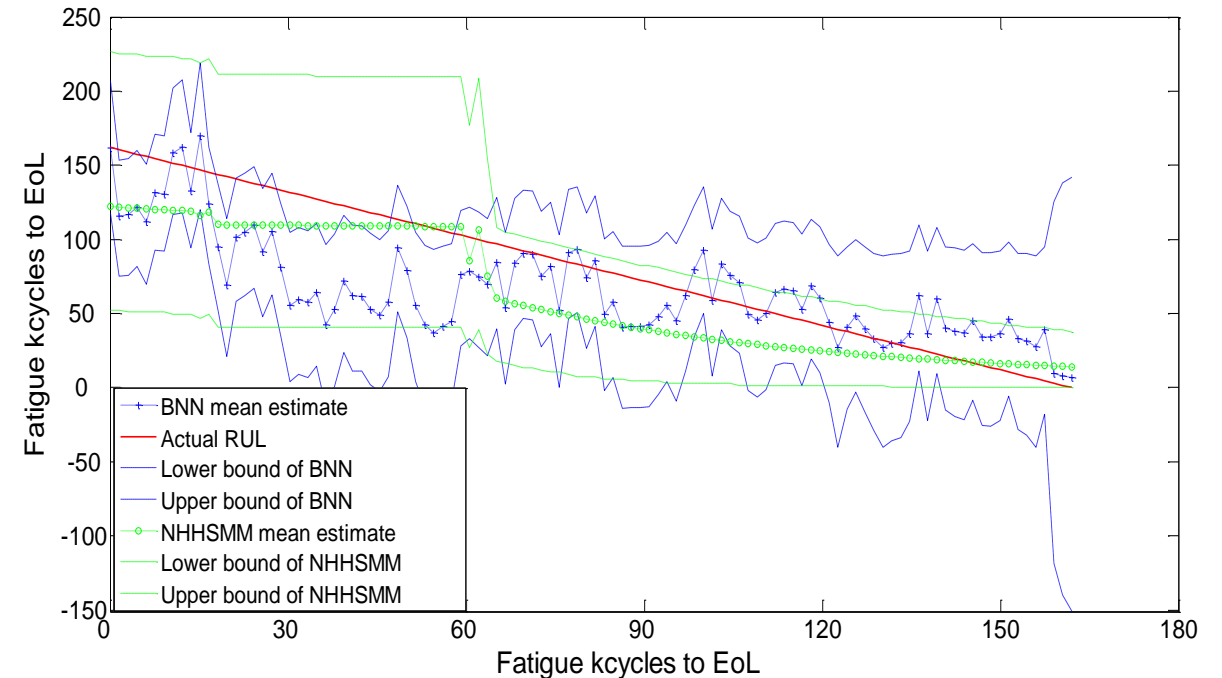
$$p(y_{new}|\mathbf{x}_{new}, \mathbf{D}) \approx \frac{1}{m} \sum_{i=1}^m p(y_{new}|\mathbf{x}_{new}, w_i)$$

Hybrid Monte-Carlo algorithm

# Results – RUL estimates



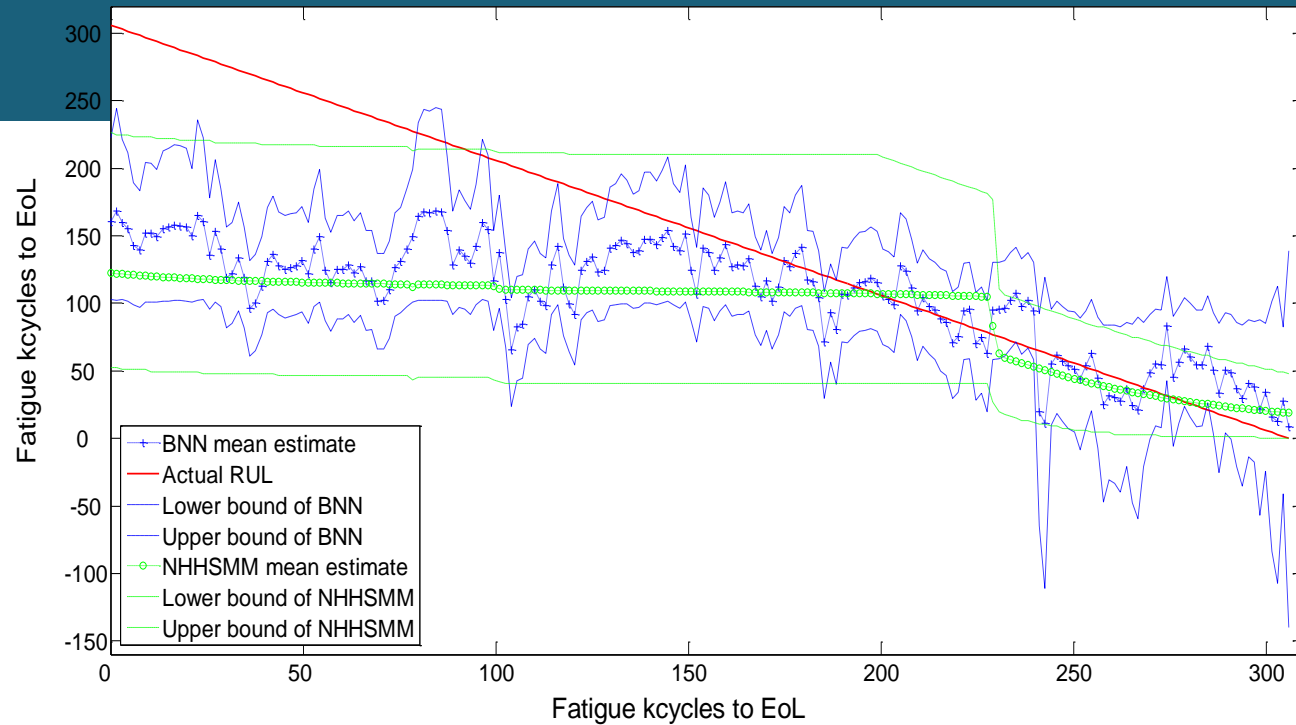
Mean and median estimations of RUL with 90% confidence intervals for coupon A2



Mean and median estimations of RUL with 90% confidence intervals for coupon A9

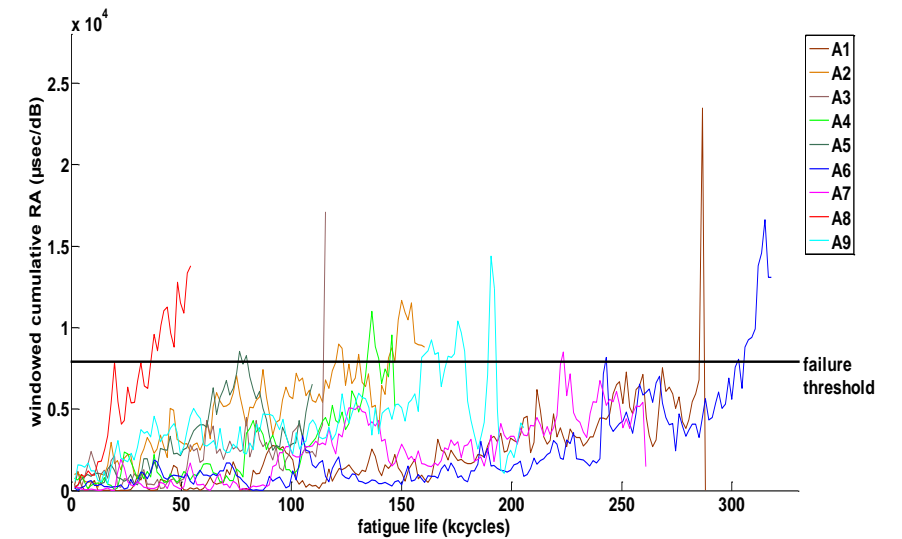
- ✓ Both models give very good predictions even from early on
- ✓ NHHSMM predictions are smoother – BNN predictions more “volatile”
- ✓ CIs get more narrow as more AE data come into play for the NHHSMM model

*Loutas et al., Composite Structures, 2016*

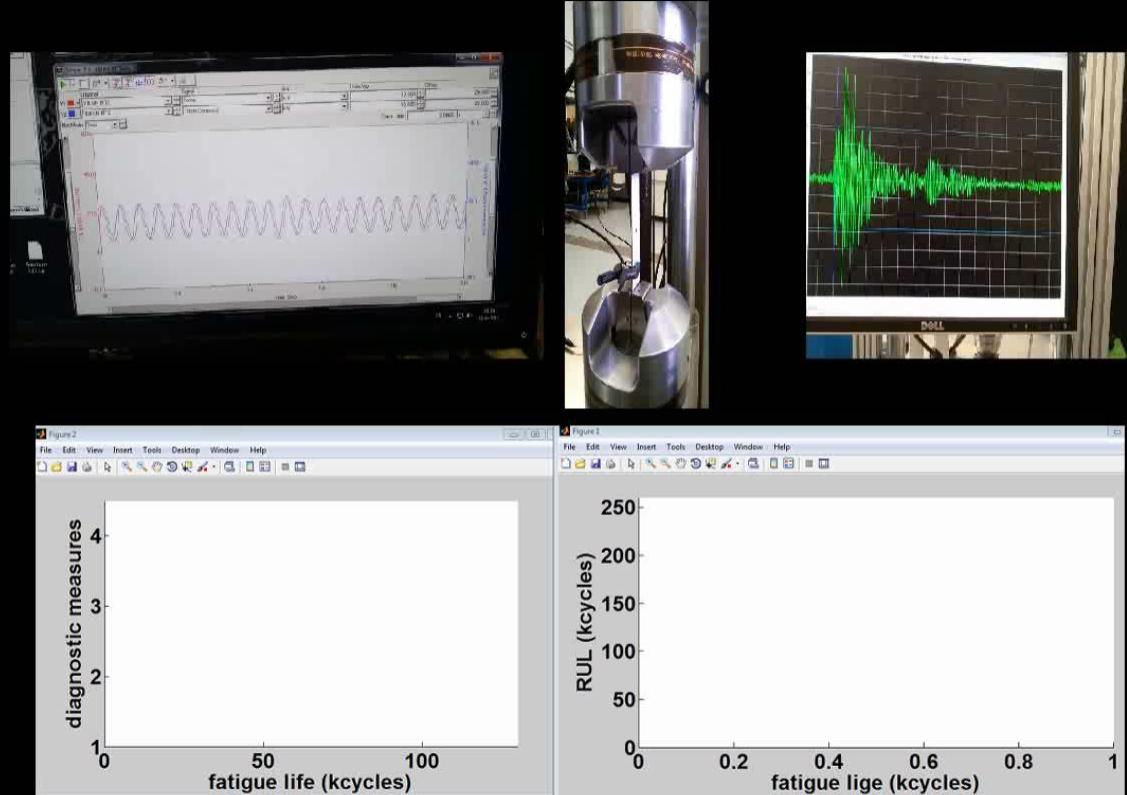


Mean and median estimations of RUL with 90% confidence intervals for coupon A6

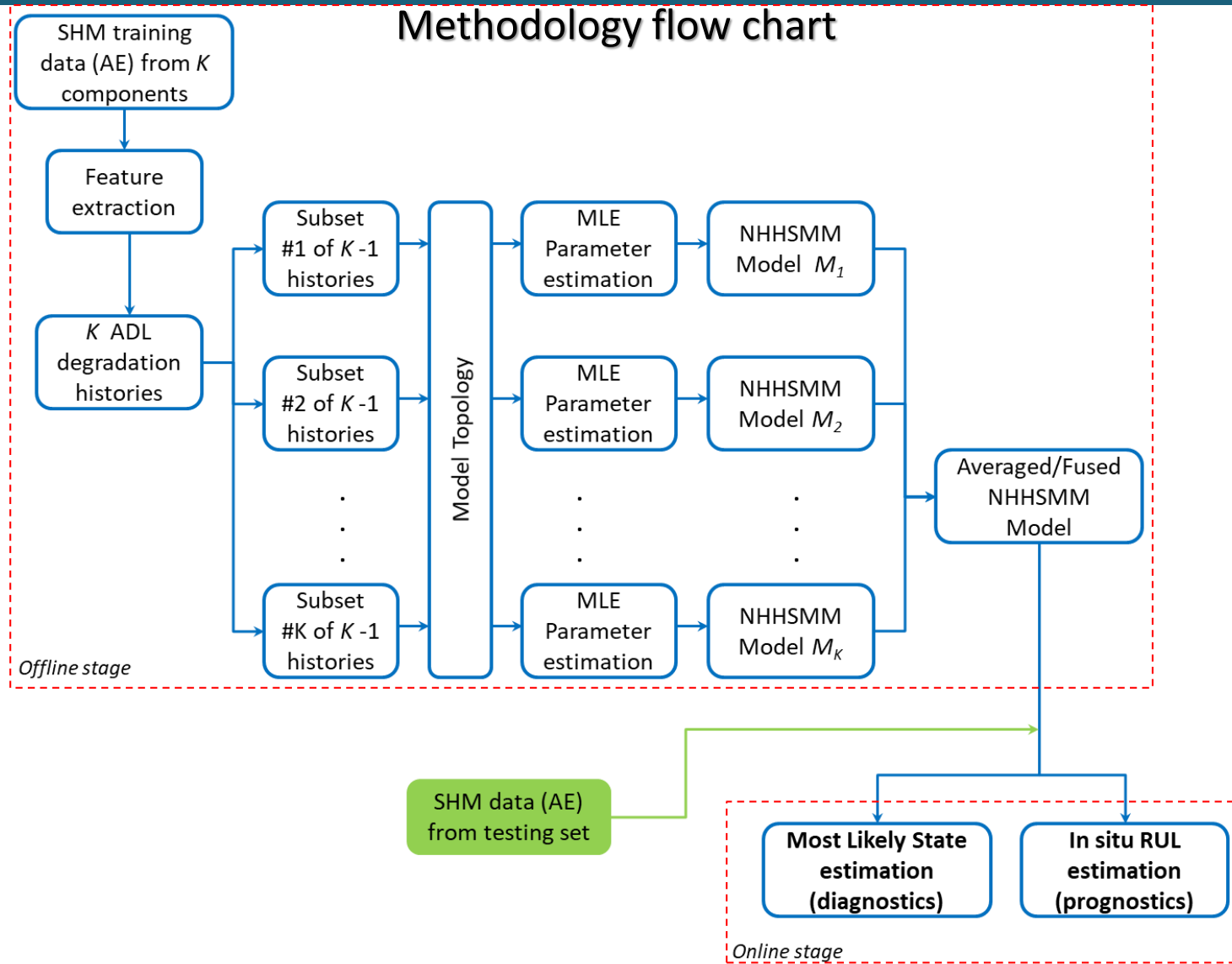
Outlier data-set, still predictions start to converge to the ground truth after mid-life



# Demonstration video







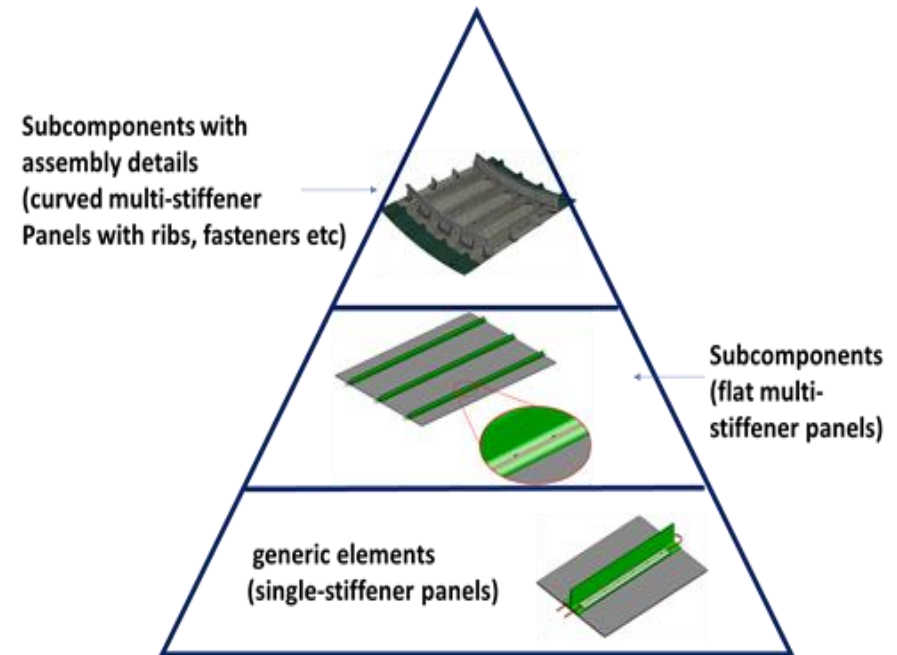
# Current challenges for SHM (in aeronautics)



- ✓ *Extra cost, non-quantified benefits, weight penalty*
- ✓ *Lack of robust diagnostic/prognostic methodologies under changing environment or extreme loadings*
- ✓ *Validation / Verification / Standardization*
- ✓ *Long-term sensors reliability/durability*
- ✓ *Lack of databases for various damage types*
- ✓ *Lack of run-to-failure data*
- ✓ *End-of-Life threshold determination*
- ✓ *Scarcity of ground truth measurements*

## Research questions

- How feasible is confident RUL estimation based on SHM data in generic element and subcomponent level?
- How reliable are data-driven prognostic methodologies when applied to complex structures under realistic fatigue loads?
- How anomalous operations phenomena, such as impacts and low velocity collisions, can affect the RUL?



# Happy to discuss!

